



# + Sterile neutrinos for believers and non-believers

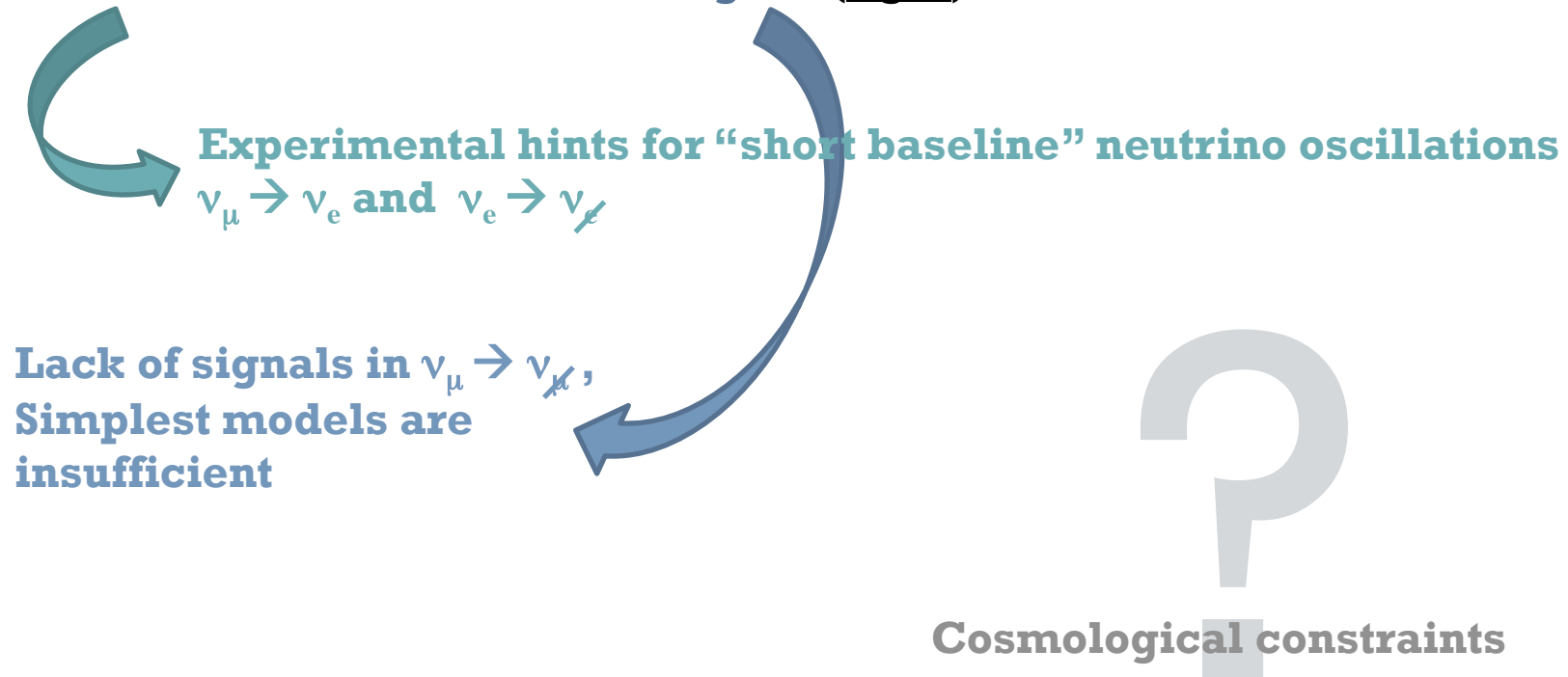
Georgia Karagiorgi, Columbia U.

FNAL Theoretical Physics Seminar  
June 27, 2013

# Outline

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## 1. Evidence for and shortcomings of (light) sterile neutrino oscillations



## 2. Future phenomenological tests of sterile neutrino models

# No sterile neutrinos in “Standard Model\*”

*\*Minimally* extended to account for neutrino mass

# Three-Neutrino Oscillation Parameters

**3 “flavor” states**

**3 “mass” states**

weak (“flavor”) states

“mass” states

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3}e^{i\delta} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

3×3 unitary mixing matrix  $U$

# Three-Neutrino Oscillation Parameters

5

**1. Why 3 “flavor” states?**

**2. Why 3 “mass” states?**

weak (“flavor”) states

“mass” states

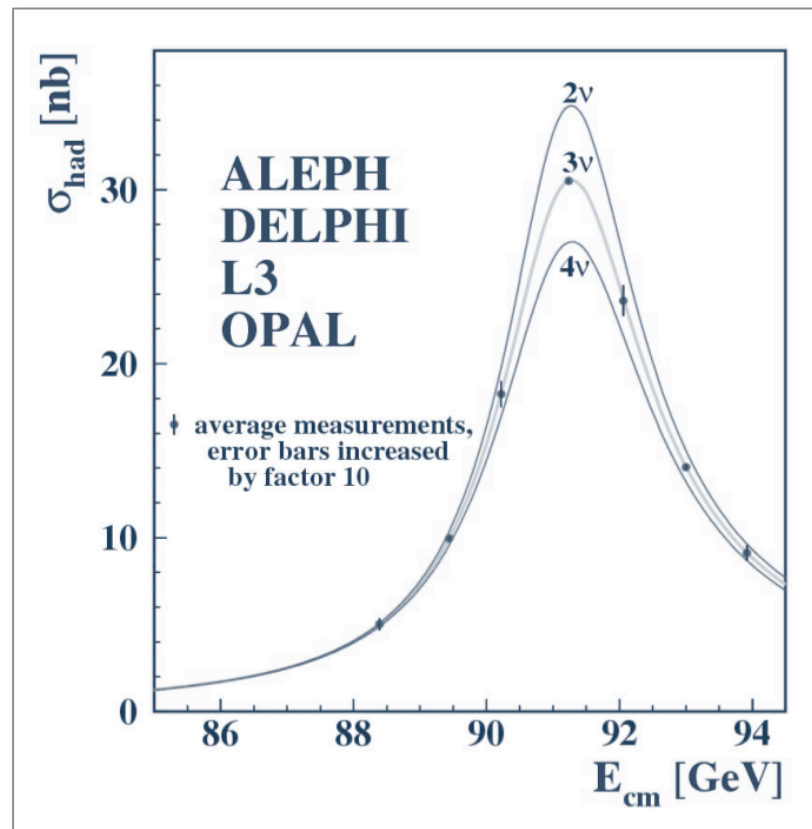
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3×3 unitary mixing matrix  $U$

# Three-Neutrino Oscillation Parameters

6

## 1. Why 3 “flavor” states?



$$N_\nu = \frac{\Gamma_{\text{inv}}}{\Gamma_\ell} \left( \frac{\Gamma_\ell}{\Gamma_\nu} \right)_{\text{SM}} = 2.984 \pm 0.008$$

[Phys. Reports 427, 257 (2006)]

Measurement of the invisible Z width:  $Z \rightarrow \nu \bar{\nu}$

# Three-Neutrino Oscillation Parameters

## 2. Why 3 “mass” states?

### 1. Theoretical prejudice

### 2. Limits on number of light neutrino species

from cosmology

Model	Data	$N_{eff}$
$N_{eff}$	W-5+BAO+SN+ $H_0$	$4.13^{+0.87(+1.76)}_{-0.85(-1.63)}$
	W-5+LRG+ $H_0$	$4.16^{+0.76(+1.60)}_{-0.77(-1.43)}$
	W-5+CMB+BAO+XLF+ $f_{gas}+H_0$	$3.4^{+0.6}_{-0.5}$
	W-5+LRG+maxBCG+ $H_0$	$3.77^{+0.67(+1.37)}_{-0.67(-1.24)}$
	W-7+BAO+ $H_0$	$4.34^{+0.86}_{-0.88}$
	W-7+LRG+ $H_0$	$4.25^{+0.76}_{-0.80}$
	W-7+ACT	$5.3 \pm 1.3$
	W-7+ACT+BAO+ $H_0$	$4.56 \pm 0.75$
	W-7+SPT	$3.85 \pm 0.62$
	W-7+SPT+BAO+ $H_0$	$3.85 \pm 0.42$
	W-7+ACT+SPT+LRG+ $H_0$	$4.08^{(+0.71)}_{(-0.68)}$
	W-7+ACT+SPT+BAO+ $H_0$	$3.89 \pm 0.41$
	W-7+CMB+BAO+ $H_0$	$4.47^{(+1.82)}_{(-1.74)}$
	W-7+CMB+LRG+ $H_0$	$4.87^{(+1.86)}_{(-1.75)}$
$N_{eff}+\Omega_k$	W-7+BAO+ $H_0$	$4.61 \pm 0.96$
	W-7+ACT+SPT+BAO+ $H_0$	$4.03 \pm 0.45$
$N_{eff}+\Omega_k+f_v$	W-7+ACT+SPT+BAO+ $H_0$	$4.00 \pm 0.43$
$N_{eff}+f_v+w$	W-7+CMB+BAO+ $H_0$	$3.68^{(+1.90)}_{(-1.84)}$
	W-7+CMB+LRG+ $H_0$	$4.87^{(+2.02)}_{(-2.02)}$
$N_{eff}+\Omega_k+f_v+w$	W-7+CMB+BAO+SN+ $H_0$	$4.2^{+1.10(+2.00)}_{-0.61(-1.14)}$
	W-7+CMB+LRG+SN+ $H_0$	$4.3^{+1.40(+2.30)}_{-0.54(-1.09)}$

[pre-Planck data: arXiv:1204.5379]

# Three-Neutrino Oscillation Parameters

Mixing matrix parameterization for two-mass-scale dominance scenario:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3}e^{i\delta} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



three mixing angles:

$$U = \underbrace{\begin{pmatrix} \cos\theta_{12} & \sin\theta_{12} & 0 \\ -\sin\theta_{12} & \cos\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\substack{\text{"solar"} \\ \theta_{12} \approx 34^\circ}} \times \underbrace{\begin{pmatrix} \cos\theta_{13} & 0 & e^{-i\delta_{CP}} \sin\theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta_{CP}} \sin\theta_{13} & 0 & \cos\theta_{13} \end{pmatrix}}_{\substack{\text{"reactor"} \\ \theta_{13} = 9^\circ}} \times \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{23} & \sin\theta_{23} \\ 0 & -\sin\theta_{23} & \cos\theta_{23} \end{pmatrix}}_{\substack{\text{"atmospheric"} \\ \theta_{23} \approx 45^\circ}}$$

a CP-violating phase:

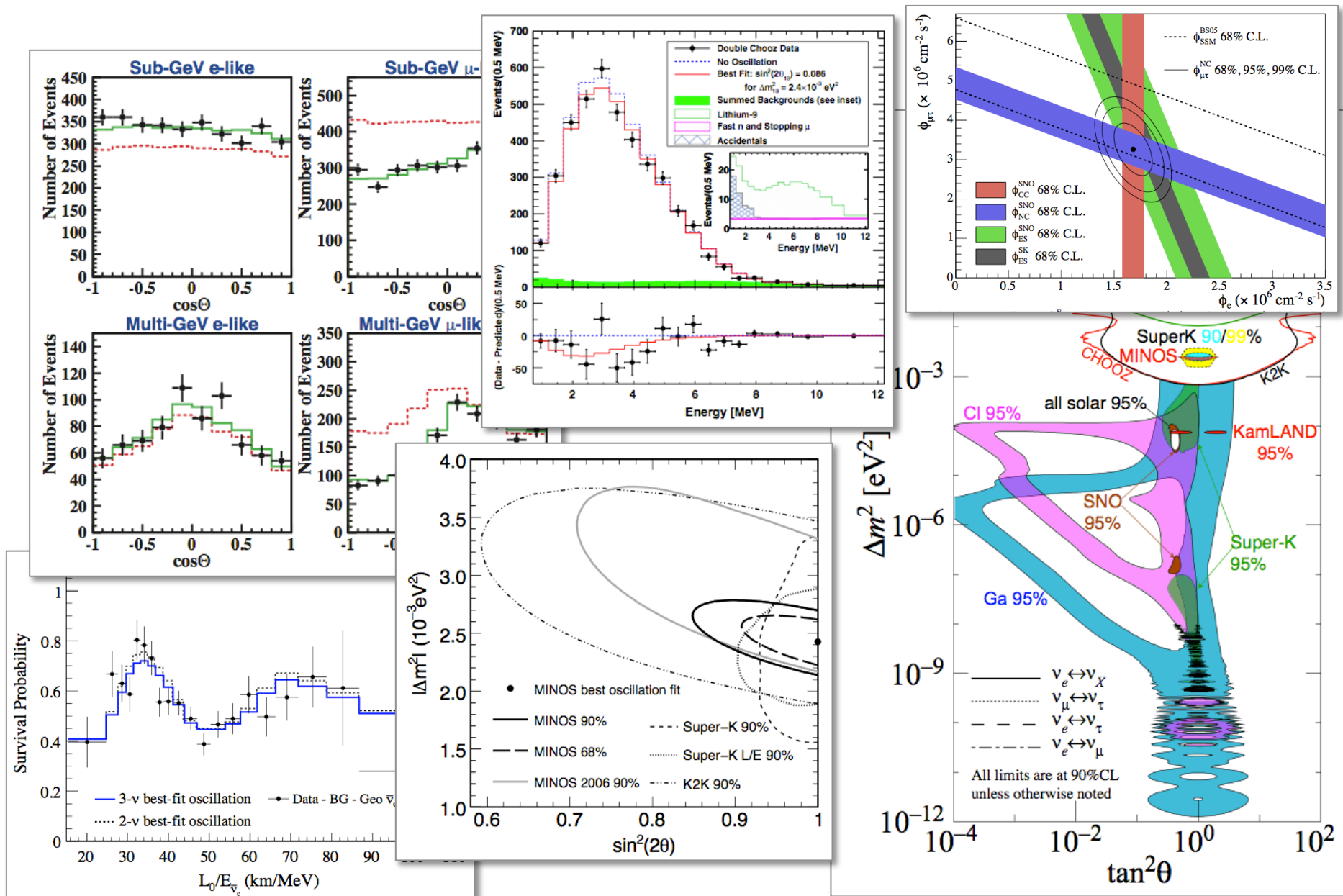
If  $\delta \neq 0$ , then have CP violation  $\Rightarrow P(\nu_\mu \rightarrow \nu_e) \neq P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$

and three mass parameters:

$m_1, m_2, m_3 \rightarrow$  two independent  $\Delta m^2$



# Evidence for three-neutrino picture



# Three-Neutrino Oscillation Parameters

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three mixing angles?

*As of 2012, the only unknown parameter!*

$$U = \begin{pmatrix} \cos\theta_{12} & \sin\theta_{12} & 0 \\ -\sin\theta_{12} & \cos\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} \cos\theta_{13} & 0 & e^{-i\delta_{CP}}\sin\theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta_{CP}}\sin\theta_{13} & 0 & \cos\theta_{13} \end{pmatrix} \times \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{23} & \sin\theta_{23} \\ 0 & -\sin\theta_{23} & \cos\theta_{23} \end{pmatrix}$$

“solar”  
 $\theta_{12} \approx 34^\circ$ 
“reactor”  
 $\theta_{13} = 9^\circ$ 
“atmospheric”  
 $\theta_{23} \approx 45^\circ$

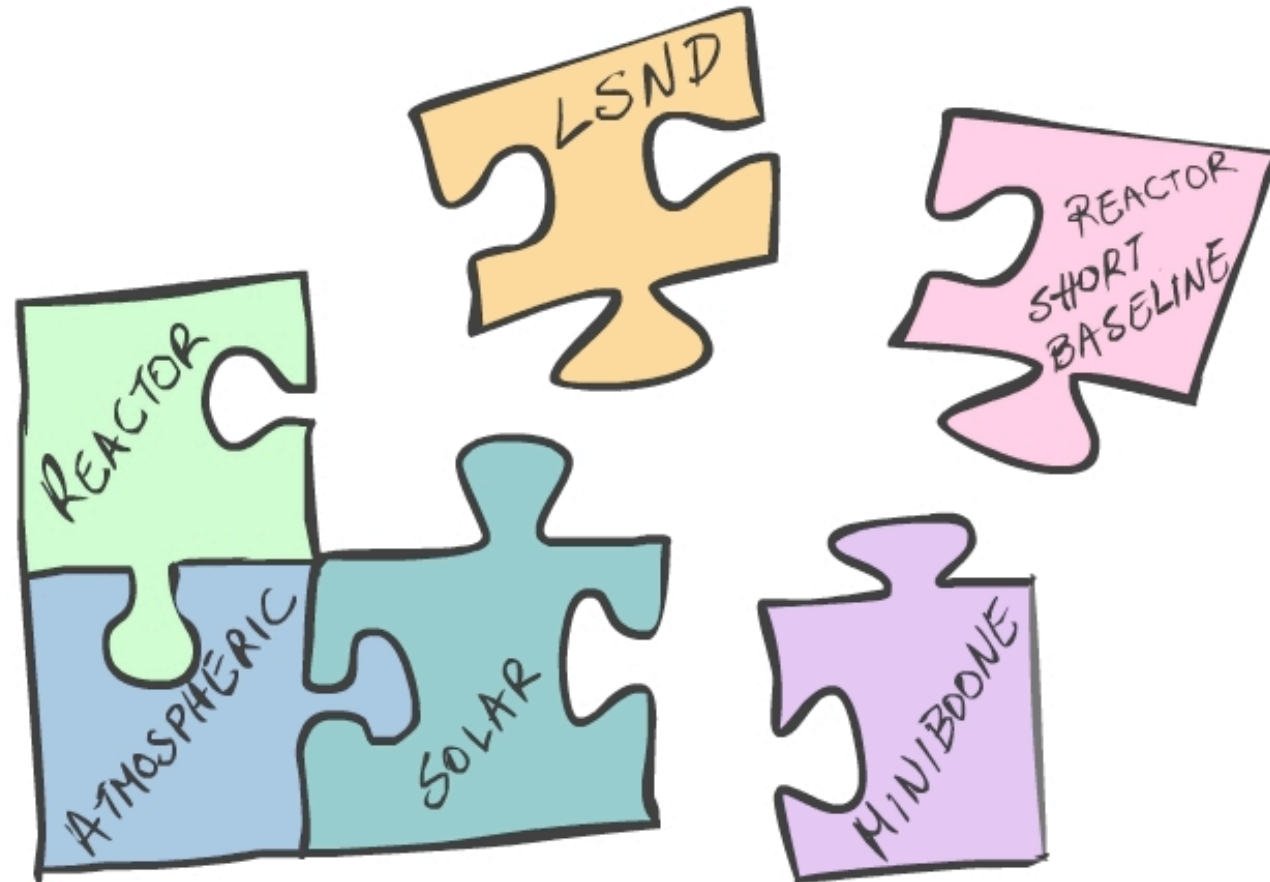
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and three mass parameters:

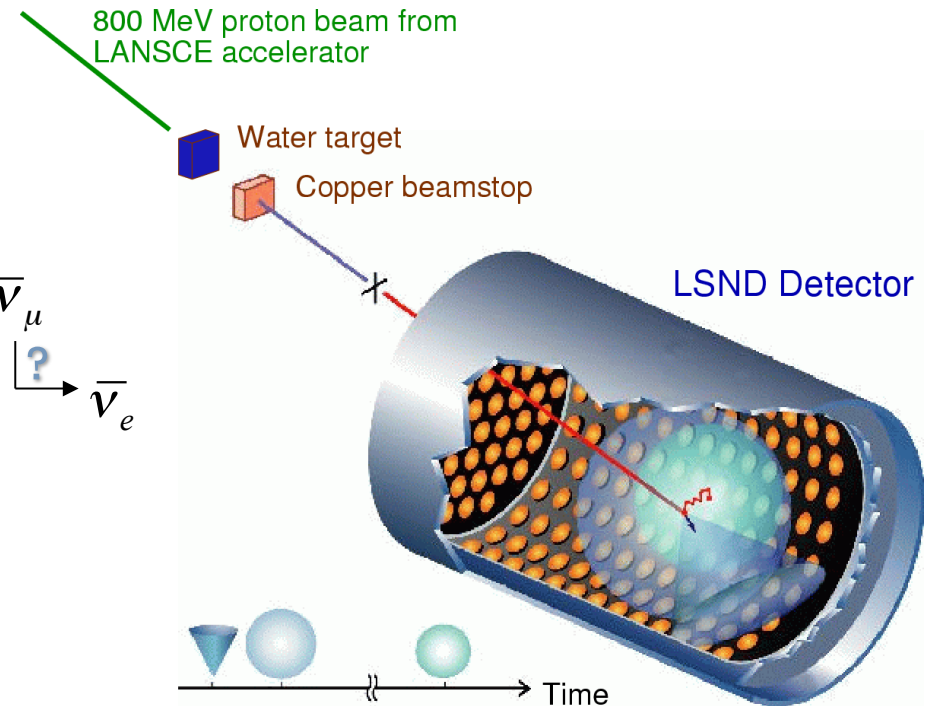
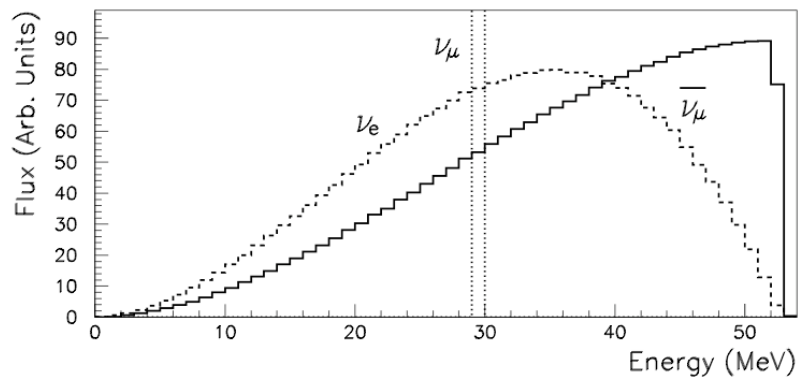
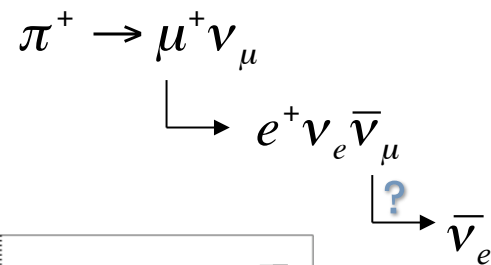
$m_1, m_2, m_3 \rightarrow$  two independent  $\Delta m^2$

# Why, or, why not sterile neutrinos?



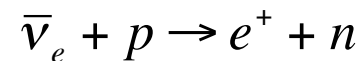
# Puzzle piece #1: LSND Experiment

$\mu^+$  decay-at-rest experiment:



Well-predicted neutrino flux and cross-section.  
Very low  $\bar{\nu}_e$  backgrounds.

$\bar{\nu}_e$  detection via inverse-beta-decay:  
(coincidence signal)



# Puzzle piece #1: LSND Experiment

$\mu^+$  decay-at-rest experiment:

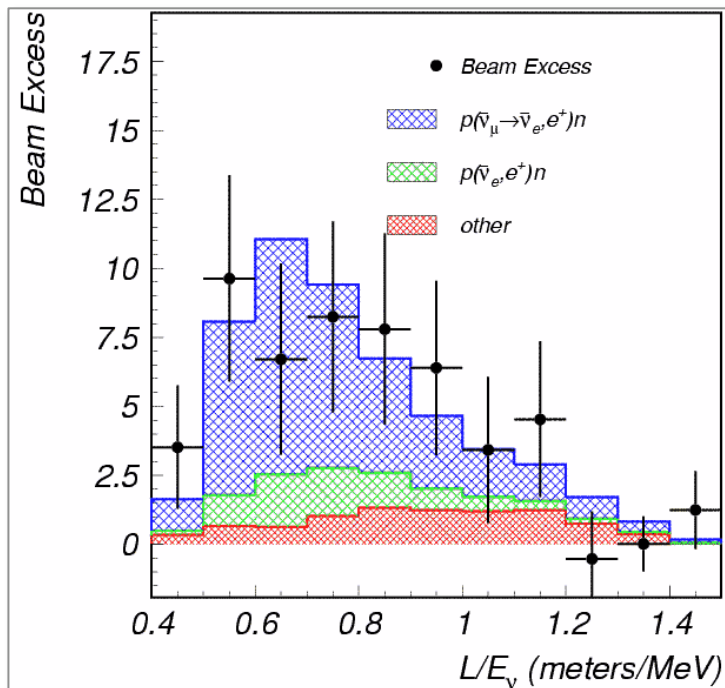
$$\pi^+ \rightarrow \mu^+ \nu_\mu$$

$$\downarrow$$

$$e^+ \nu_e \bar{\nu}_\mu$$

$$\downarrow ?$$

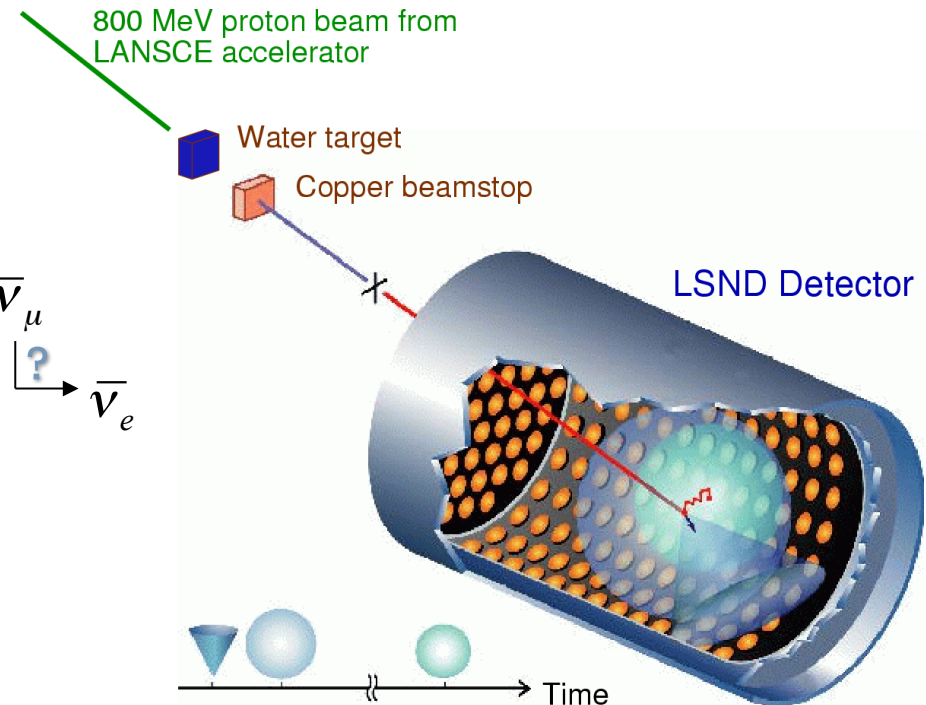
$$\bar{\nu}_e$$



Observed excess of  $\bar{\nu}_e$   
described by oscillation probability:

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = (0.264 \pm 0.067 \pm 0.045) \%$$

(3.8 $\sigma$  evidence)

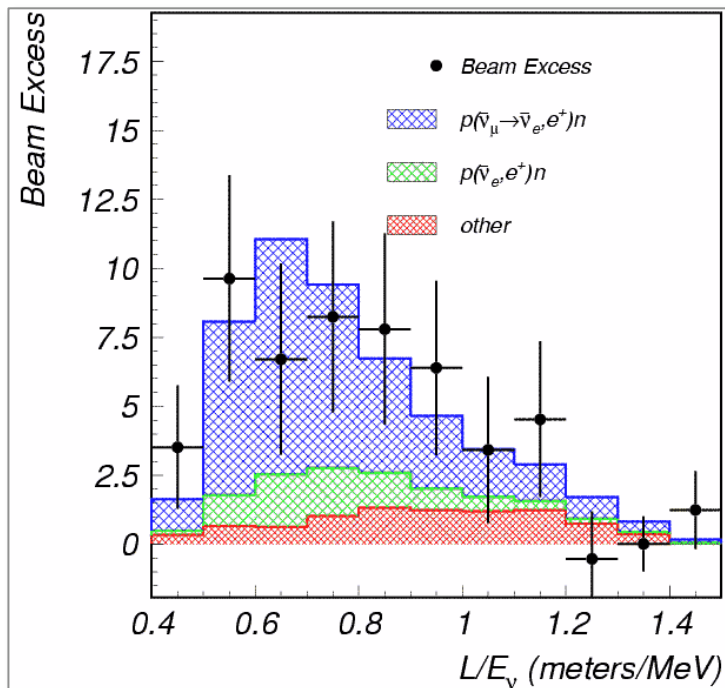


[C. Athanassopoulos et al., Phys. Rev. Lett. 75, 2650 (1995);  
81,1774(1998); A.Aguilaret al., Phys. Rev. D64, 112007(2001).]

# Puzzle piece #1: LSND Experiment

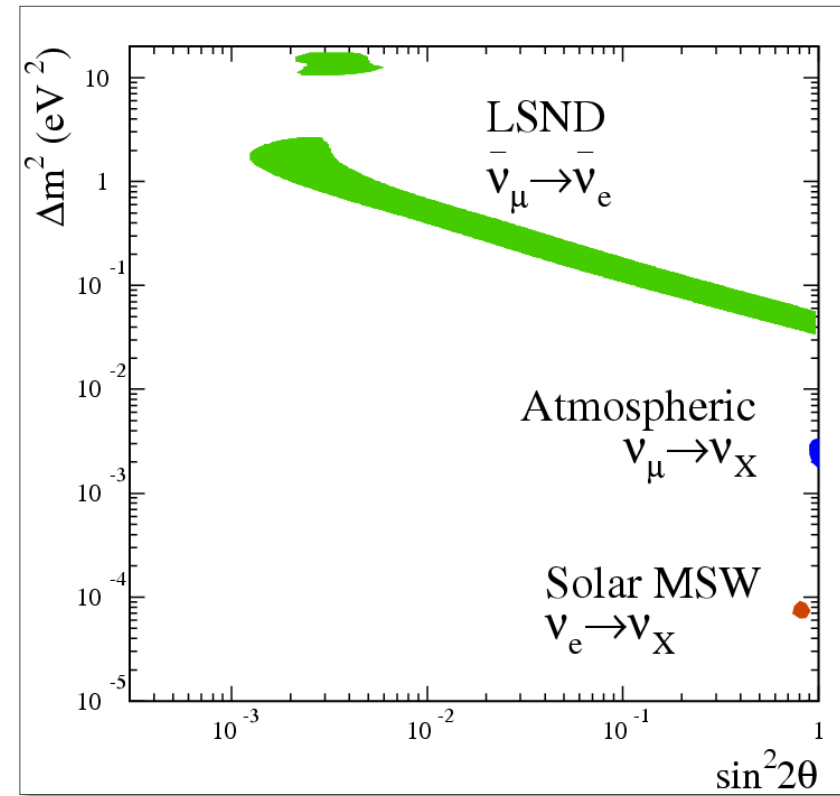
Points to large  $\Delta m^2$   
if interpreted as  
two-neutrino oscillations:

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\vartheta_{\mu e} \sin^2(1.27 \Delta m^2 L / E)$$



Observed excess of  $\bar{\nu}_e$   
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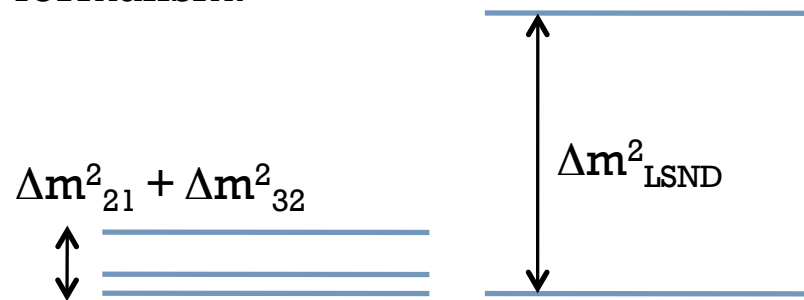
[C. Athanassopoulos et al., Phys. Rev. Lett. 75, 2650 (1995);  
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# Puzzle piece #1: LSND Experiment

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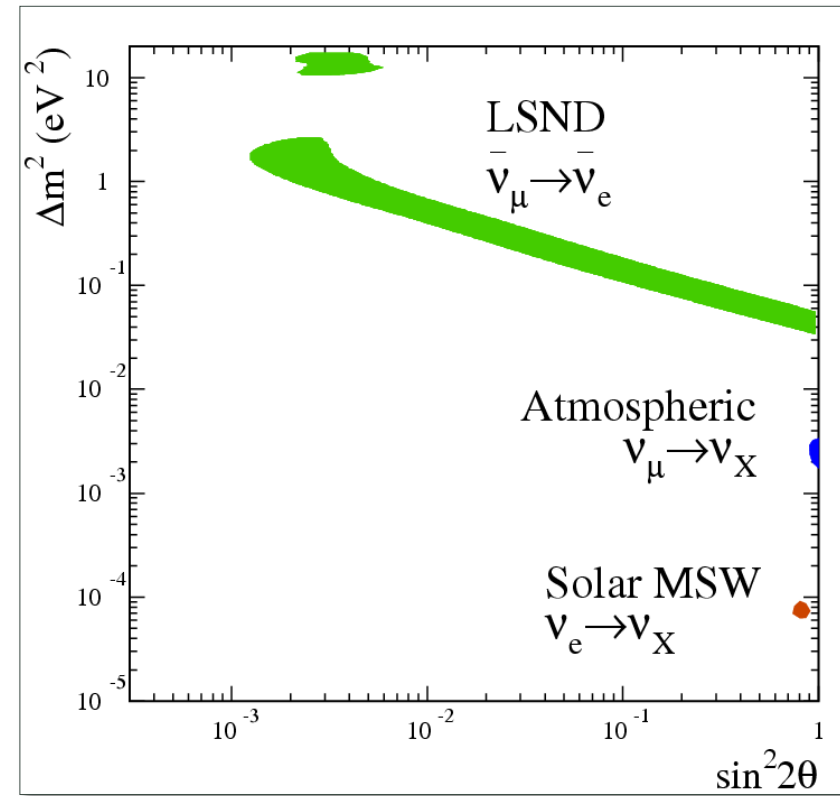
$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\vartheta_{\mu e} \sin^2(1.27 \Delta m^2 L / E)$$

In conflict with three-neutrino  
formalism!



$$\Delta m^2_{\text{LSND}} \gg \Delta m^2_{21} + \Delta m^2_{32}$$

**Needs more than 3 neutrino mass states!**

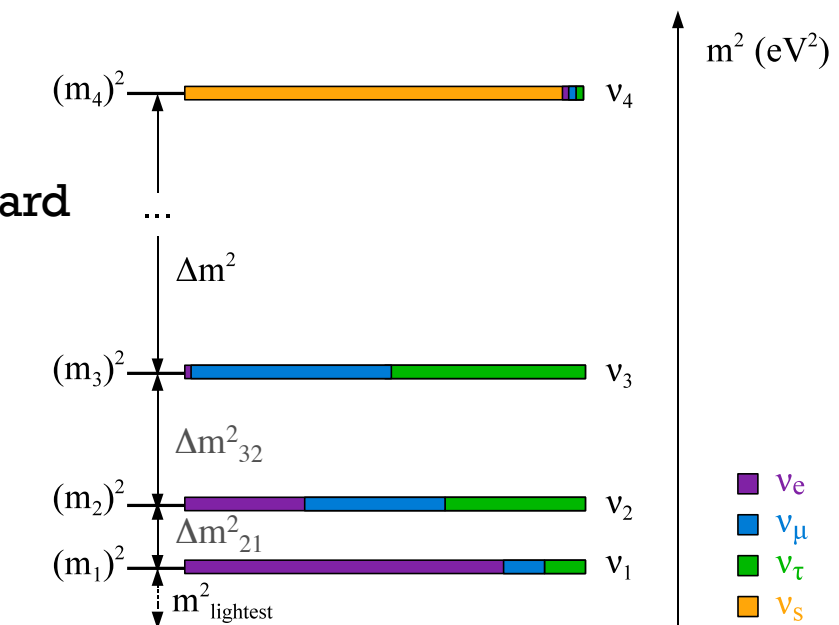


# Possible interpretation: sterile neutrino

Additional neutrino “flavor” (and mass) state which has **no weak interactions** (through the standard W/Z bosons)

Additional mass state is assumed to be produced through mixing with the standard model neutrinos

→ Can affect neutrino oscillations through mixing





# Sterile Neutrino Oscillation Formalism

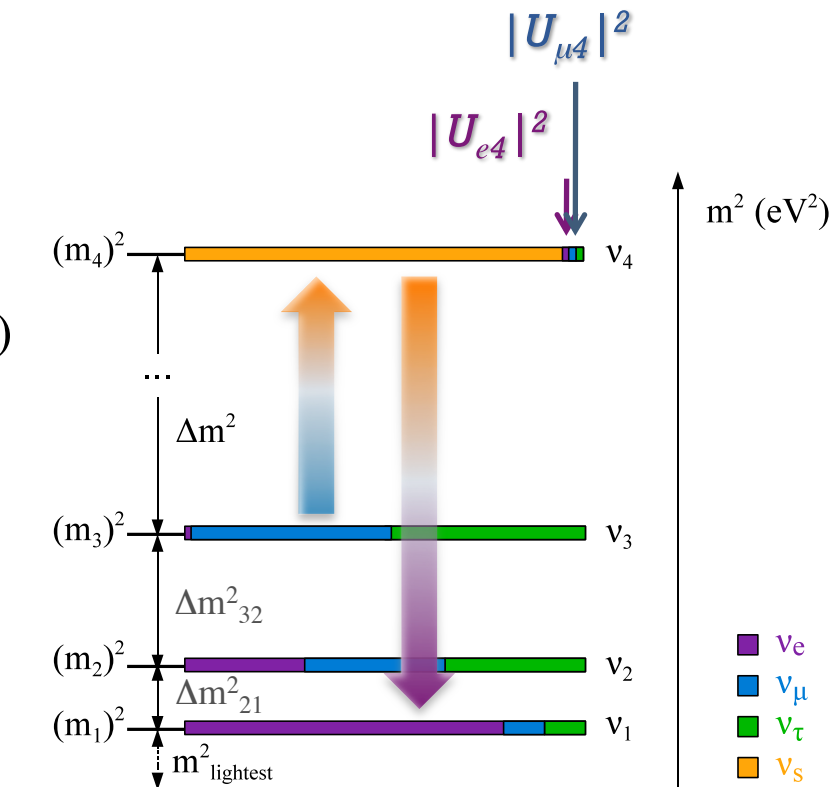
## Oscillation effects:

$\nu_\mu \rightarrow \nu_e$  appearance\*:

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\vartheta_{\mu e} \sin^2(1.27 \Delta m^2 L / E)$$

$$\searrow \quad 4|U_{e4}|^2|U_{\mu4}|^2$$

**Explains LSND result**

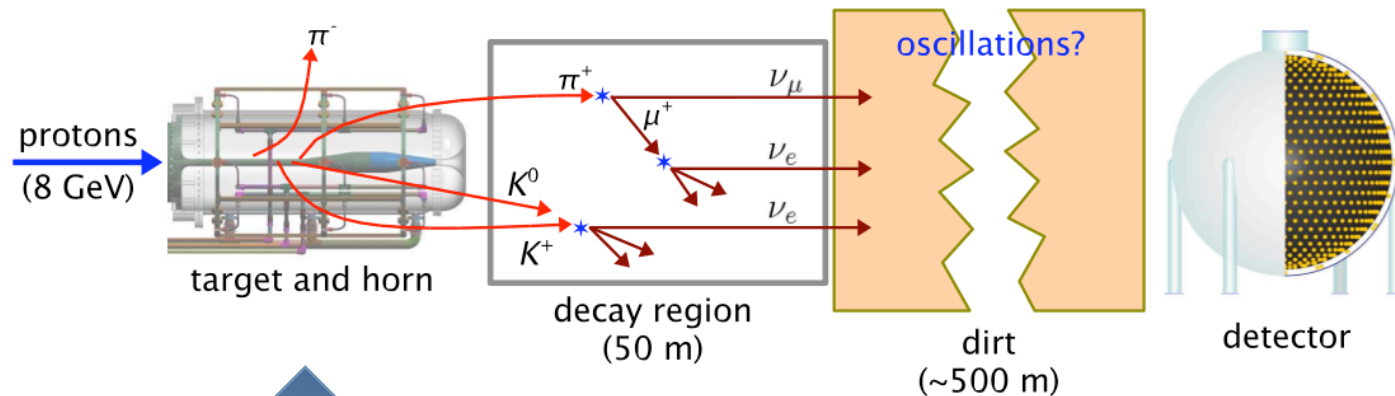


(3+1)

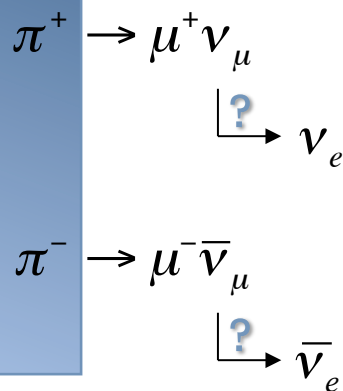
\*Approximation:  $m_1, m_2, m_3 \ll m_4 \rightarrow m_1, m_2, m_3 = 0$

# Puzzle piece #2: MiniBooNE

MiniBooNE was proposed to independently test the LSND oscillation hypothesis:



magnetic field polarity  
selects  $\nu$  or  $\bar{\nu}$

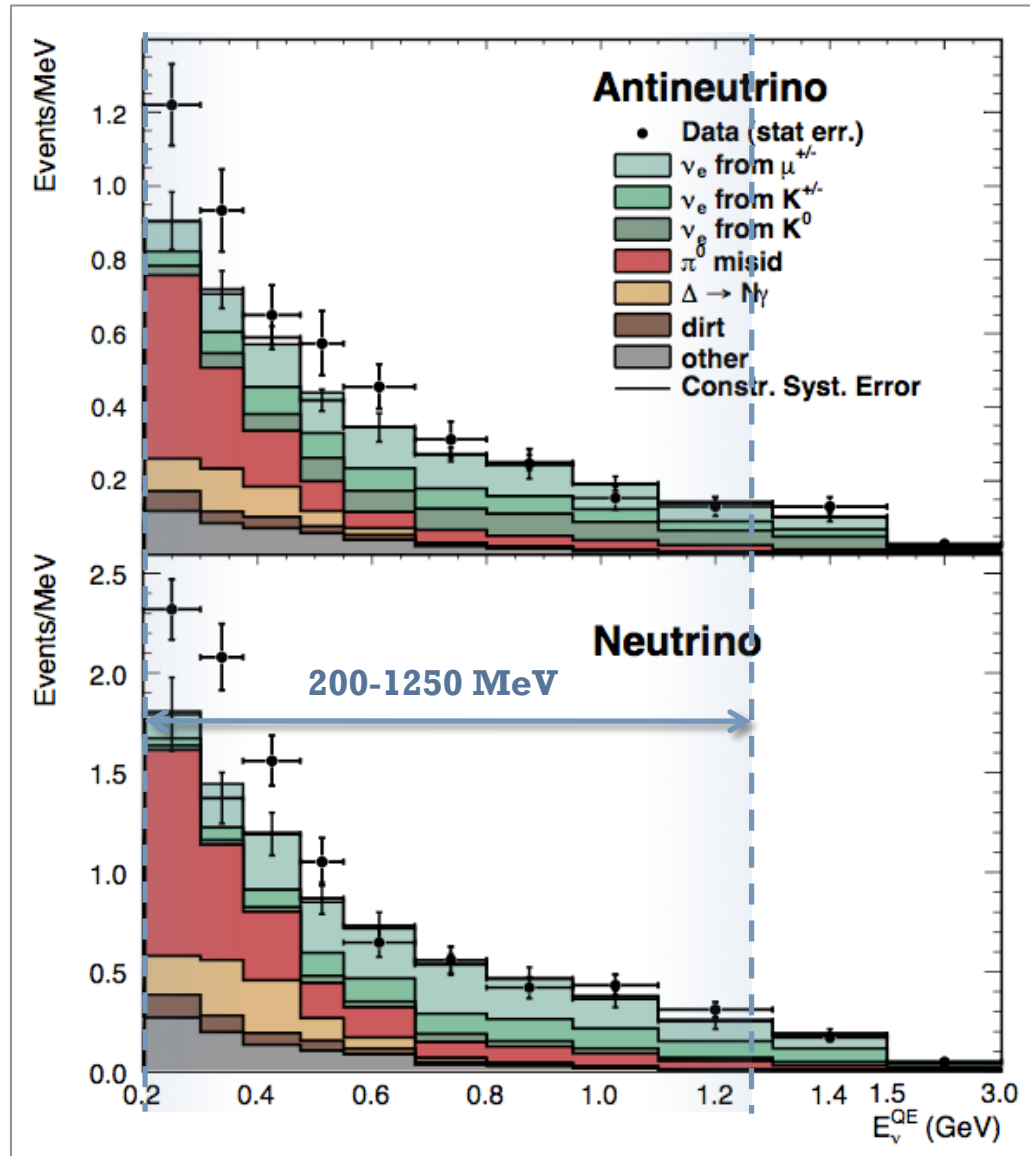


Similar L/E as LSND

but

- Different energy, beam and detector systematics
- Different event signatures and backgrounds (cherenkov detector)

# Puzzle piece #2: MiniBooNE



[arXiv:1303.2588, submitted to Phys. Rev. Lett.;  
see also:

Phys.Rev.Lett.110:161801,2012

Phys.Rev.Lett.98:231801,2007,

Phys.Rev.Lett.102:101802,2009,

Phys.Rev.Lett.103:111801,2009,

Phys.Rev.Lett.105:181801,2010]

**Oscillation signal region:**  
**200-1250 MeV**

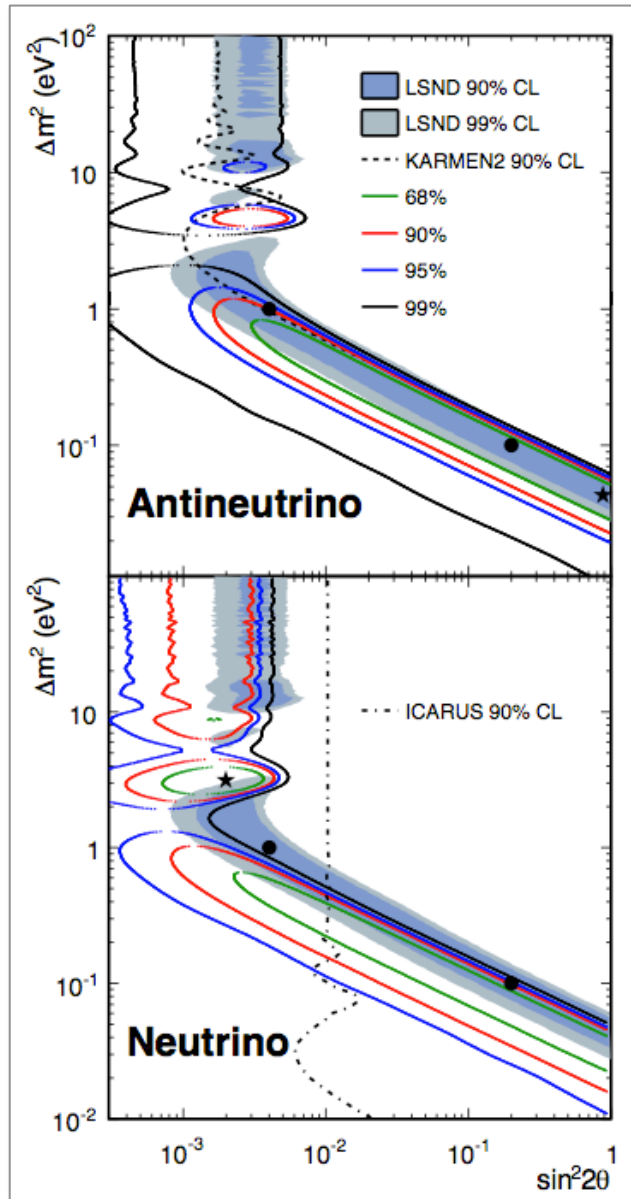
**Antineutrino search:**  
**2.8 $\sigma$  excess**

Excess of events is at both high  
and “low energy.”

**Neutrino search:**  
**3.4 $\sigma$  excess**

Excess of events is at “low energy,”  
 $E < 475$  MeV.

# Puzzle piece #2: MiniBooNE



[arXiv:1303.2588, submitted to Phys. Rev. Lett.;  
see also:

Phys.Rev.Lett.110:161801,2012

Phys.Rev.Lett.98:231801,2007,

Phys.Rev.Lett.102:101802,2009,

Phys.Rev.Lett.103:111801,2009,

Phys.Rev.Lett.105:181801,2010]

## Antineutrino (3+1) best fit:

$\chi^2$ -probability = 66%

$(\Delta m^2, \sin^2 2\theta) = (0.04 \text{ eV}^2, 0.88)$

Background-only relative to best fit: 0.5%

## Neutrino (3+1) best fit:

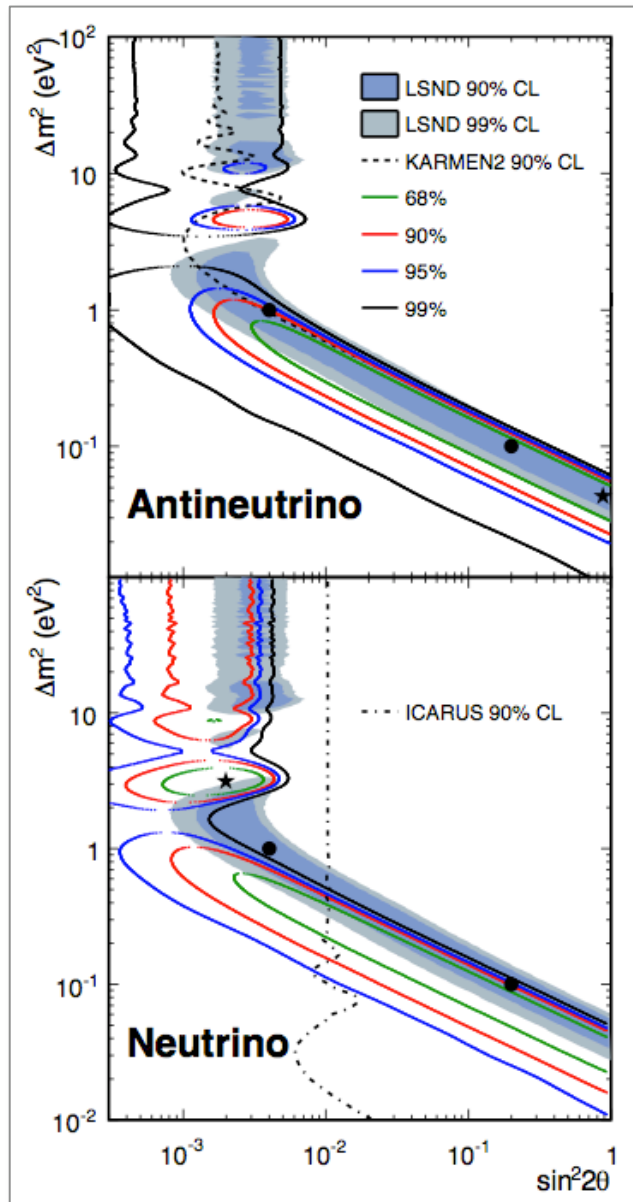
$\chi^2$ -probability = 6.1%

$(\Delta m^2, \sin^2 2\theta) = (3.14 \text{ eV}^2, 0.002)$

Background-only relative to best fit: 2%

**Both are consistent with (3+1) oscillations in general, but MiniBooNE antineutrino allowed parameters are in better agreement with LSND parameters.**

# Puzzle piece #2: MiniBooNE



Barring CP violation,

$$P(\nu_\mu \rightarrow \nu_e) \equiv P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$$

(3+1) approximation  
does not allow for CP violation

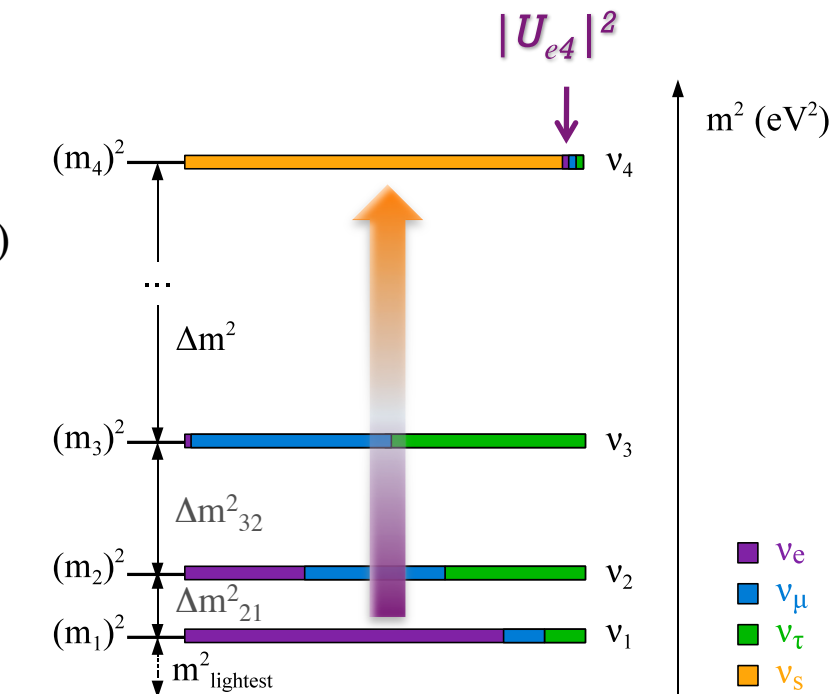
# Sterile Neutrino Oscillation Formalism

$\nu_\mu \rightarrow \nu_e$  appearance implies  $\nu_\mu$  and  $\nu_e$  disappearance!

$\nu_e$  disappearance\*:

$$P(\nu_e \rightarrow \nu_e) = 1 - \sin^2 2\vartheta_{ee} \sin^2(1.27 \Delta m^2 L / E)$$

$$\rightarrow 4|U_{e4}|^2(1 - |U_{e4}|^2)$$



(3+1)

\*Approximation:  $m_1, m_2, m_3 \ll m_4 \rightarrow m_1, m_2, m_3 = 0$

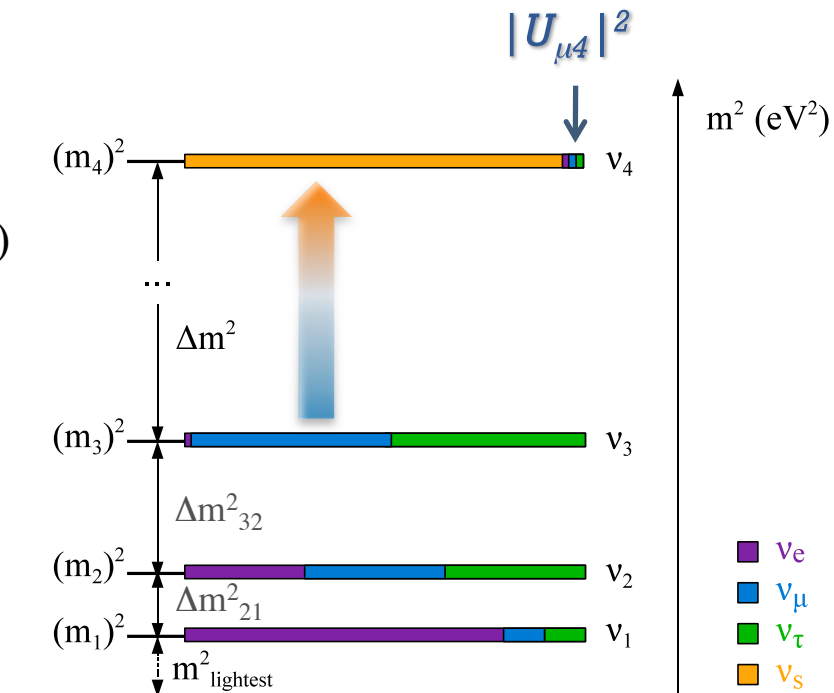
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$$\rightarrow 4|U_{\mu 4}|^2(1 - |U_{\mu 4}|^2)$$

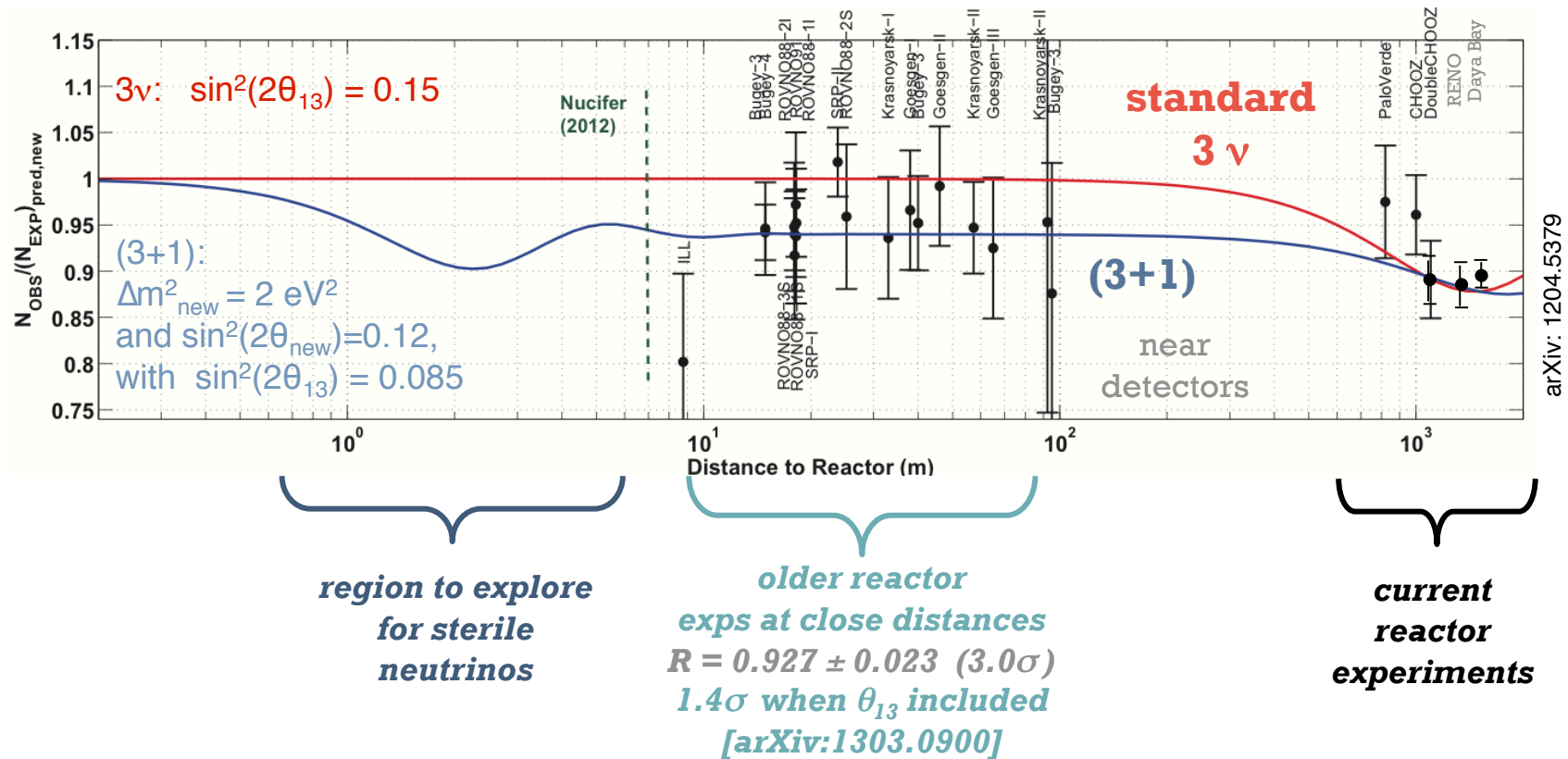


(3+1)

\*Approximation:  $m_1, m_2, m_3 \ll m_4 \rightarrow m_1, m_2, m_3 = 0$

# Puzzle piece #3: Reactor Anomaly

$\bar{\nu}_e \rightarrow \bar{\nu}_s$  disappearance?

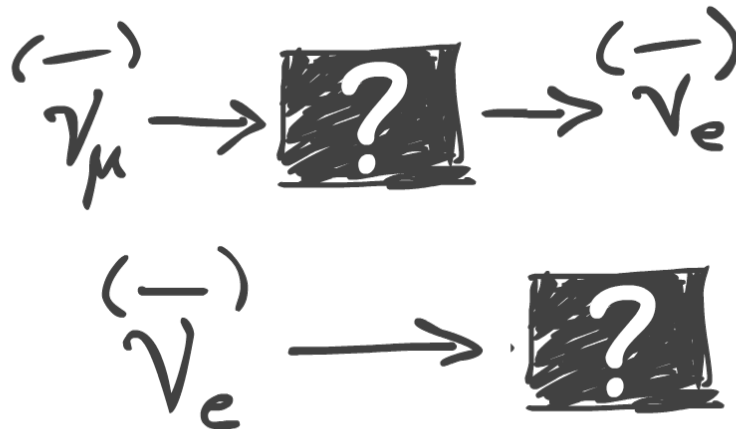


Fewer reactor neutrinos than expected at short baselines

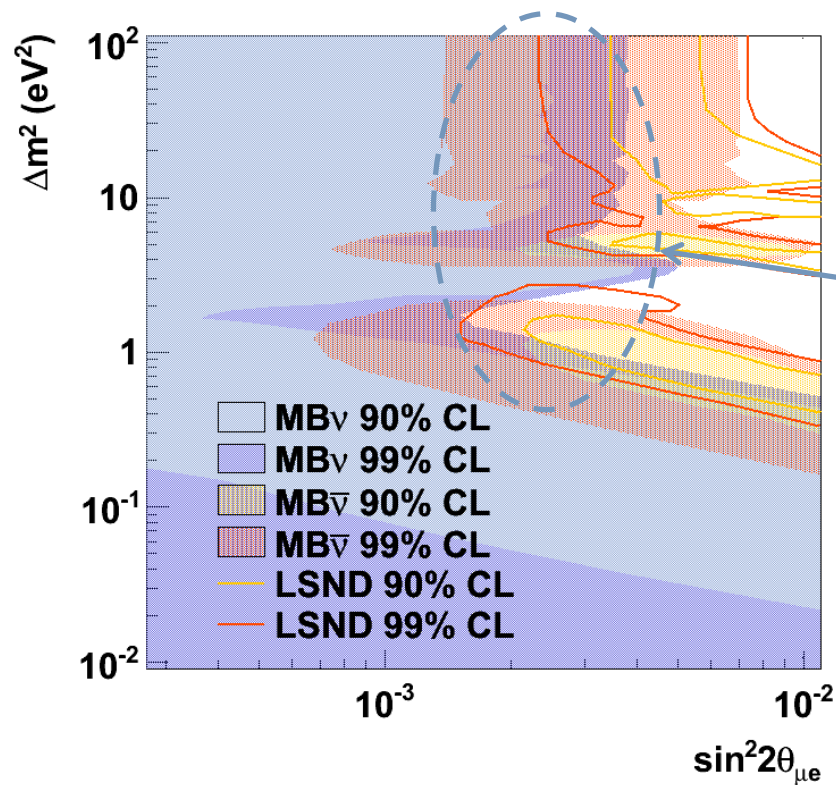
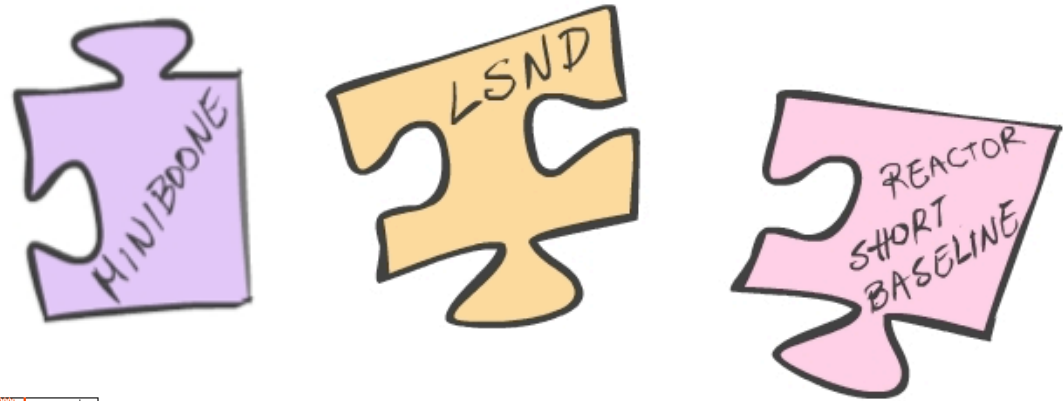
→ A possible interpretation: sterile neutrino osc. with  $\Delta m^2 \sim 1 \text{ eV}^2$  and  $\sin^2 2\theta \sim 0.1$



1. Can all three signatures be explained by (3+1) sterile neutrino hypothesis?



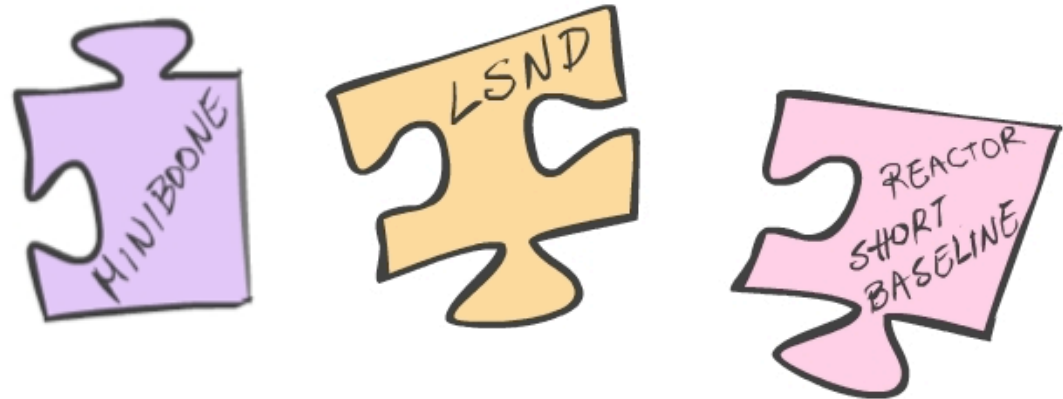
1. Can all three signatures be explained by (3+1) sterile neutrino hypothesis?



Reactor short-baseline  
consistent with these values

**A: Yes!**

1. Can all three signatures be explained by (3+1) sterile neutrino hypothesis?



2. What about information from other experiments sensitive to high- $\Delta m^2$  oscillations?

$(\bar{\nu}_\mu)$  disappearance

CDHS  
CCFR84  
SuperK/K2K (atm)  
MiniBooNE (dis)  
MINOS CC

$(\bar{\nu}_\mu) \rightarrow (\bar{\nu}_e)$  appearance

MiniBooNE  $\nu$   
MiniBooNE  $\bar{\nu}$   
LSND  
KARMEN  
NOMAD  
NuMI-MB

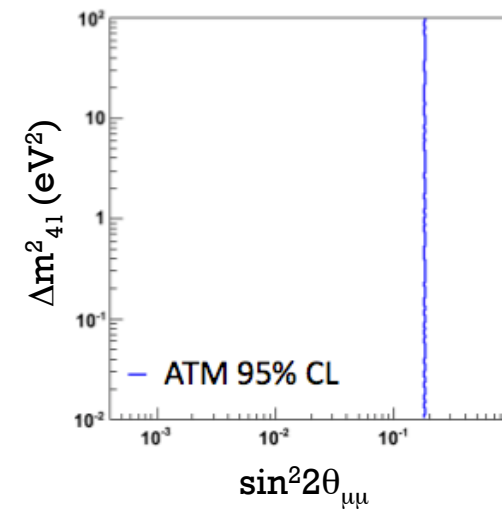
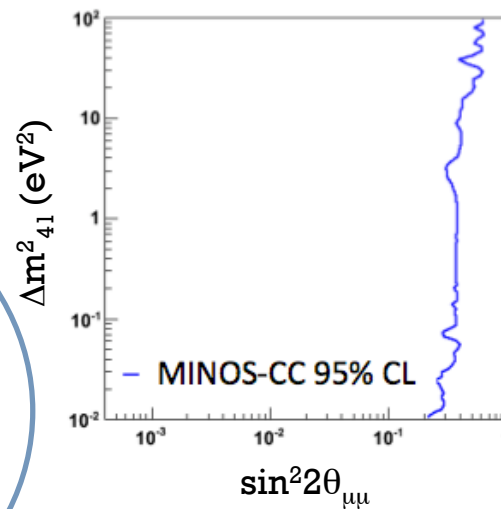
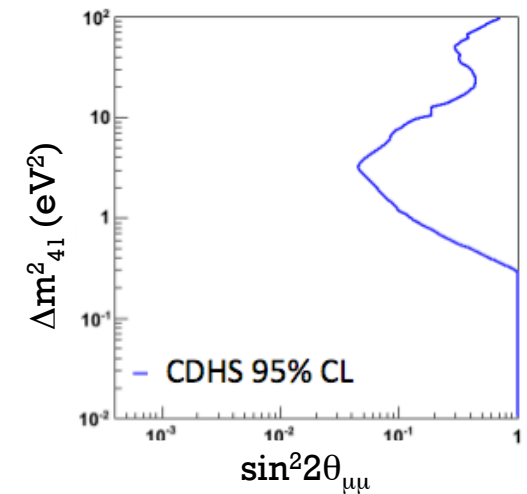
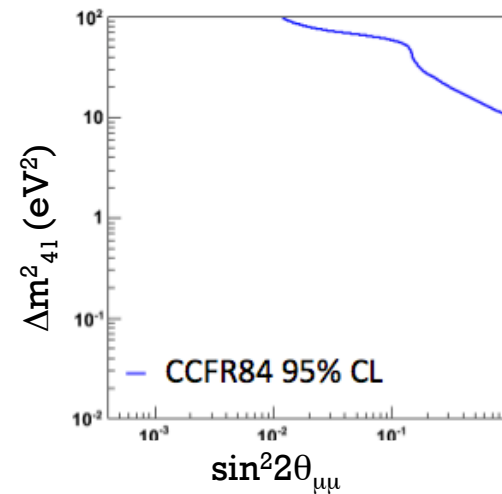
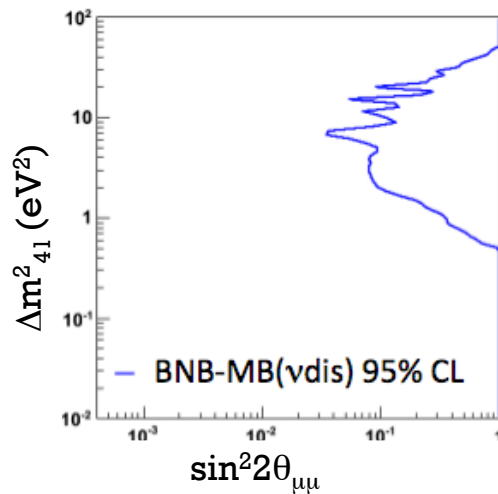
$(\bar{\nu}_e)$  disappearance

Bugey  
KARMEN/LSND (xsec)  
Gallium

[Conrad, Ignarra, GK, Shaevitz, Spitz,  
arXiv:1207.4765, accepted by Advances in HEP;  
see also:

GK et al, Phys.Rev. D80 (2009) 073001,  
GK et al, Phys.Rev. D75 (2007) 013011]

# Other experimental constraints



$(\bar{\nu}_\mu)$  disappearance

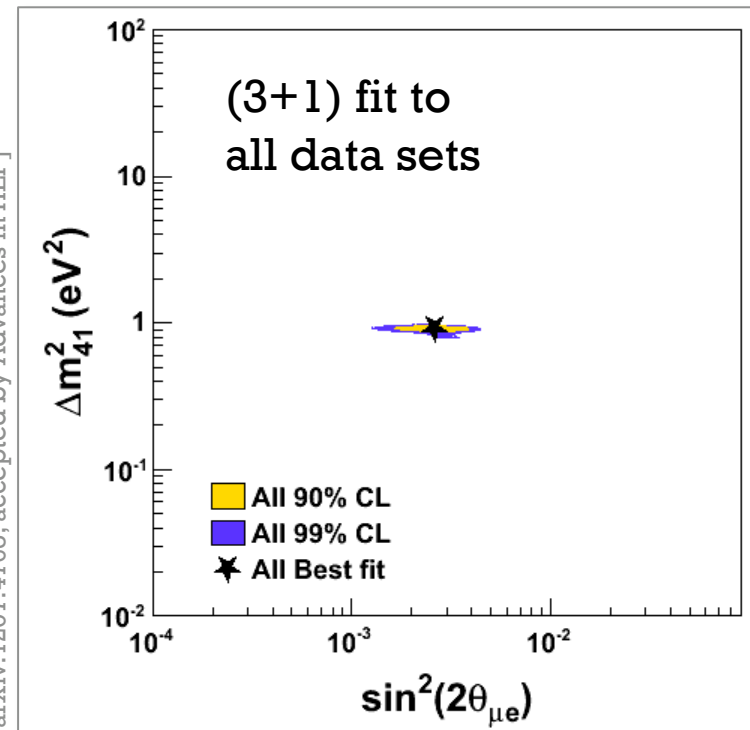
CDHS  
CCFR84  
SuperK/K2K (atm)  
MiniBooNE (dis)  
MINOS CC

# (3+1) Global Fits to Sterile Neutrino Oscillations

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<b>3+1</b>	$\Delta m_{41}^2$	$ U_{\mu 4} $	$ U_{e 4} $
All	0.92	0.17	0.15

[Conrad, Ignarra, GK, Shaevitz, Spitz,  
arXiv:1207.4765, accepted by Advances in HEP]



**Compatibility** among  
data sets included in the fit

Null  $\chi^2$  (dof)  
286.5 (240)

Null gof  
**2.1%**

Best fit  $\chi^2$  (dof)  
233.9 (237)

Best fit gof  
**55%**

PG  $\chi^2$  (dof)  
54 (24)

**PG**  
**0.043%**

# Compatibility (PG) Test

A measure of **how well the parameter regions** preferred by different subsets of data **overlap**

$$\chi^2_{PG} = \chi^2_{min,all} - \sum \chi^2_{min,i}$$

$$\text{compatibility, PG} = \text{prob}(\chi^2_{PG}, \text{ndf}_{PG})$$

Unlike a  $\chi^2$  test, the PG test avoids the problem that a possible disagreement between data sets becomes diluted by data points which are insensitive to the fit.

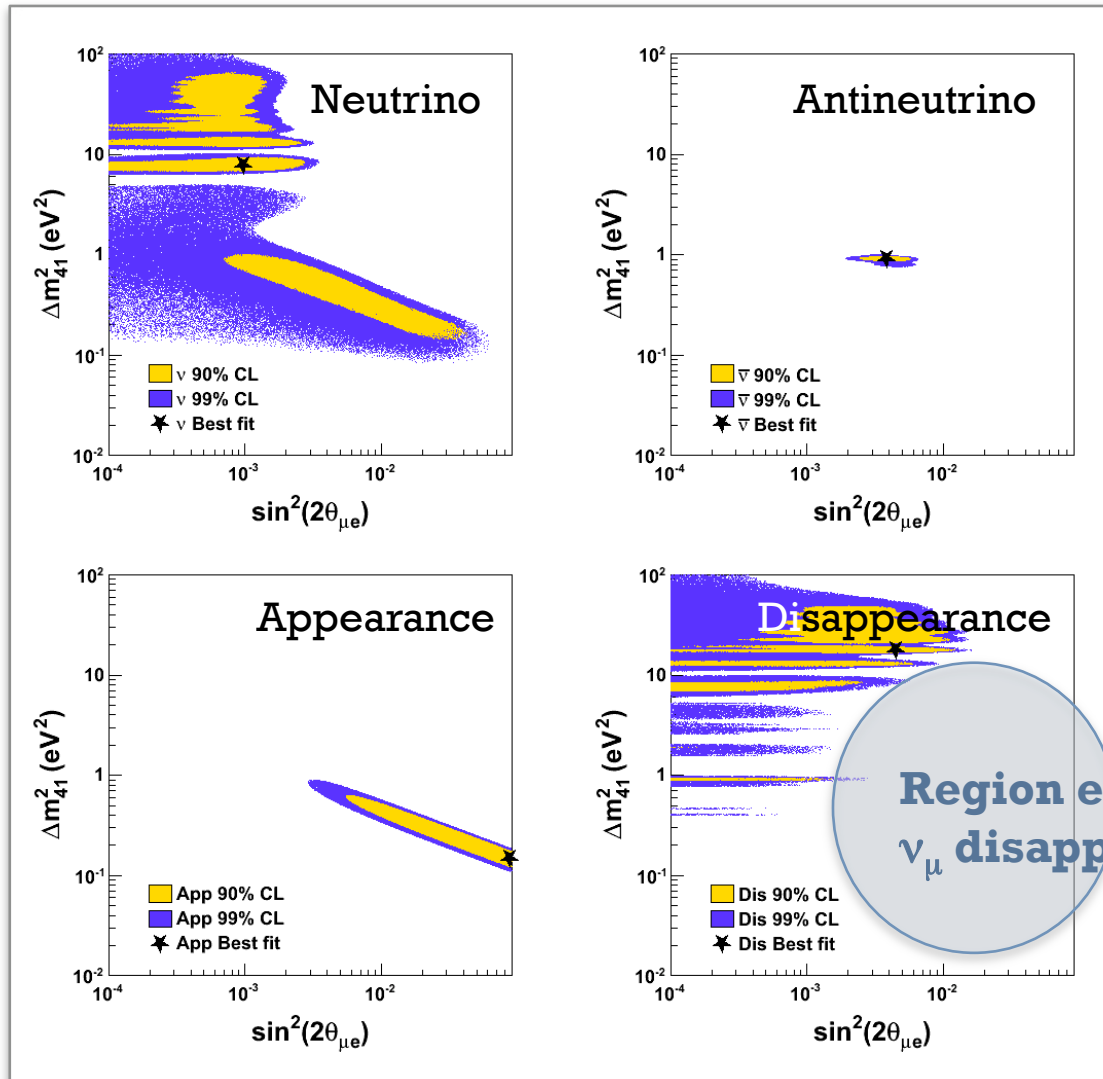
**A commonly used metric.**

“Testing the statistical compatibility of independent data sets”

Maltoni & Schwetz, Phys. Rev. D68 (2003) 033020

# (3+1) is not enough!

## Incompatibilities!



Compatibility ( $\nu, \bar{\nu}$ ) = 0.14%

Compatibility (app, dis) = 0.013%

Region excluded from  
 $\nu_\mu$  disappearance experiments

[Conrad, Ignarra, GK, Shaevitz, Spitz,  
arXiv:1207.4765, accepted by Advances in HEP]

# Global Fits: Caveats and Limitations

- Appearance searches assume no disappearance
  - This is an incorrect assumption, given best fit parameters extracted in global fits
  - This may resolve some tension seen in the MiniBooNE appearance data sets, if one allows for  $\nu_e$  background disappearance
  
- Need a more advanced statistical and systematic treatment of data sets
  - Compatibility measure needs to be verified with fake data and frequentist studies
  - Need better treatment of systematic correlations between data sets.

This is a challenging step, but necessary for meaningful quantitative statements on these models



(3+1) is not enough!

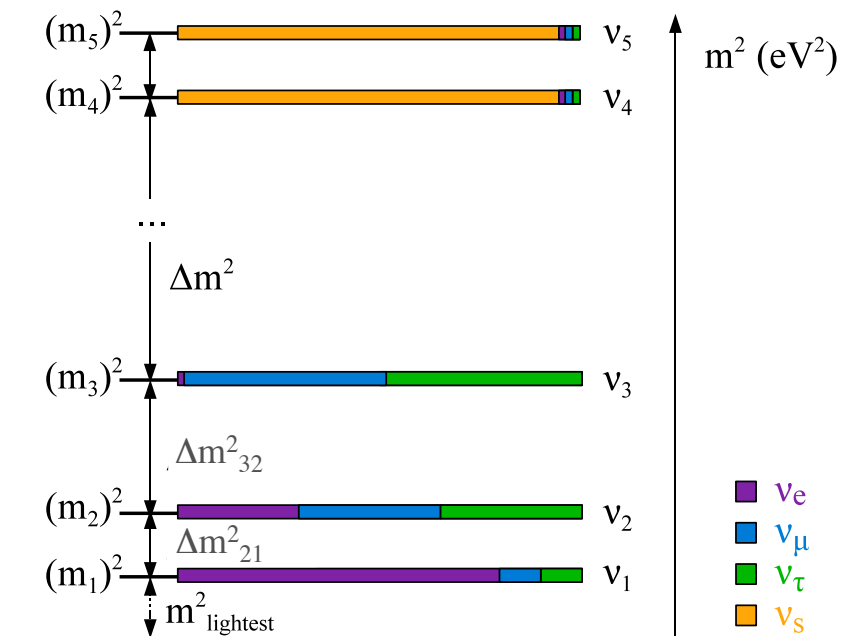
Theoretical developments attempting to address inconsistencies:

- Fact #1:  $\nu$  vs  $\bar{\nu}$  differences  
Extended sterile neutrino models with CP violation?
- Fact #2: appearance vs disappearance differences  
“Non-standard” oscillations?

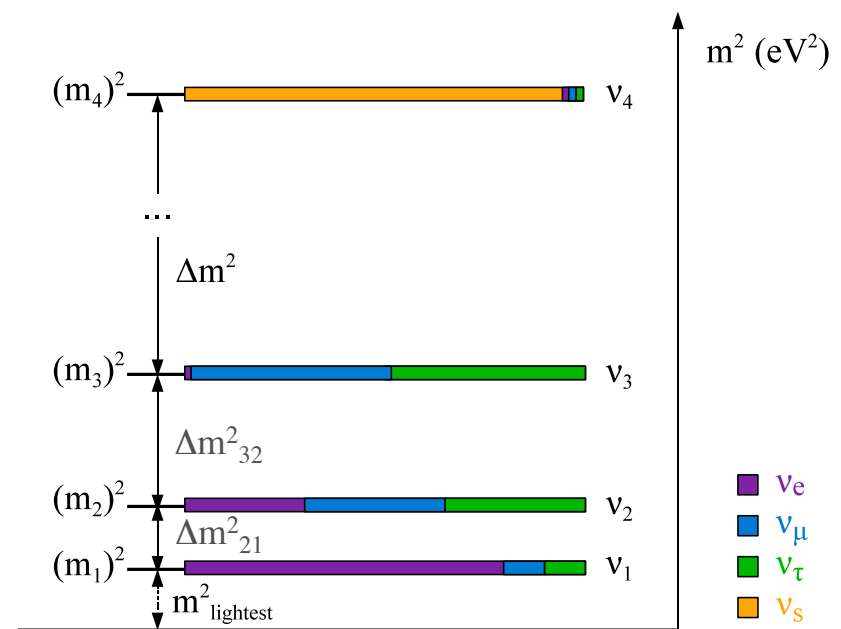
# Extended models: (1) CP violation

34

Can have **more than one new state...**



(3+2)



(3+1)

# Extended models: (1) CP violation

Disappearance:

$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - 4[(1 - |U_{\alpha 4}|^2 - |U_{\alpha 5}|^2) \cdot (|U_{\alpha 4}|^2 \sin^2 x_{41} + |U_{\alpha 5}|^2 \sin^2 x_{51}) + |U_{\alpha 4}|^2 |U_{\alpha 5}|^2 \sin^2 x_{54}]$$

Appearance:

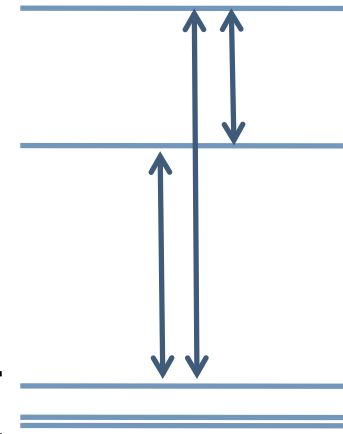
$$P(\nu_\alpha \rightarrow \nu_{\beta \neq \alpha}) = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2 \sin^2 x_{41} + 4|U_{\alpha 5}|^2 |U_{\beta 5}|^2 \sin^2 x_{51} + 8|U_{\alpha 5}| |U_{\beta 5}| |U_{\alpha 4}| |U_{\beta 4}| \sin x_{41} \sin x_{51} \cos(x_{54} - \phi_{45})$$

$$x_{ji} \equiv 1.27 \Delta m_{ji}^2 L/E$$

CPV phase

assumed degenerate

→ 2 effective  $\Delta m^2$



**(3+2)** is attractive because of **CP violation**

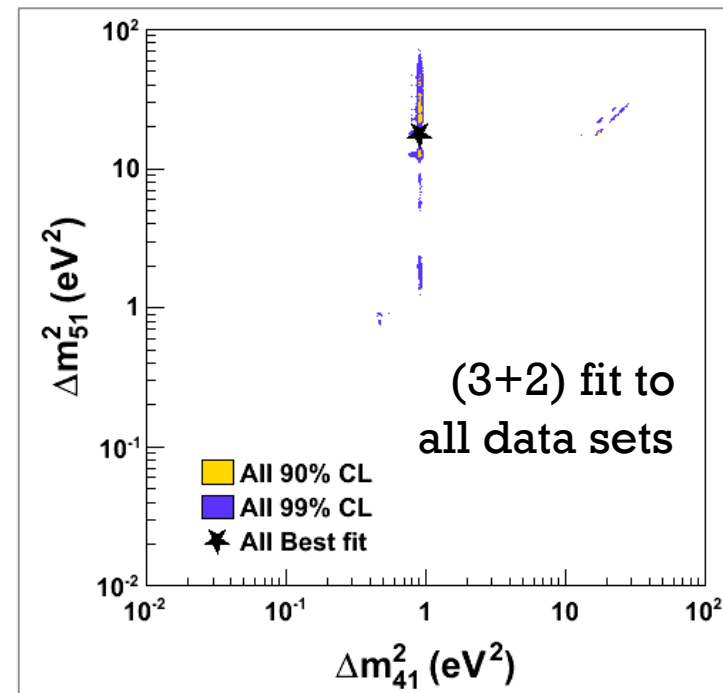
# Extended models: (1) CP violation

## (3+2): Global Fit

**PG** ( $\nu, \bar{\nu}$ ) = 5.3%

**PG** (app, dis) = 0.0082%

Conrad et al, hep-ph/1207.4765



3+2	$\Delta m_{41}^2$	$\Delta m_{51}^2$	$ U_{\mu 4} $	$ U_{e 4} $	$ U_{\mu 5} $	$ U_{e 5} $	$\phi_{54}$
All	0.92	17	0.13	0.15	0.16	0.069	$1.8\pi$

**Compatibility** among  
data sets included in the fit

Null  $\chi^2$  (dof)  
286.5 (240)

Null gof  
**2.1%**

Best fit  $\chi^2$  (dof)  
221.5 (233)

Best fit gof  
**69%**

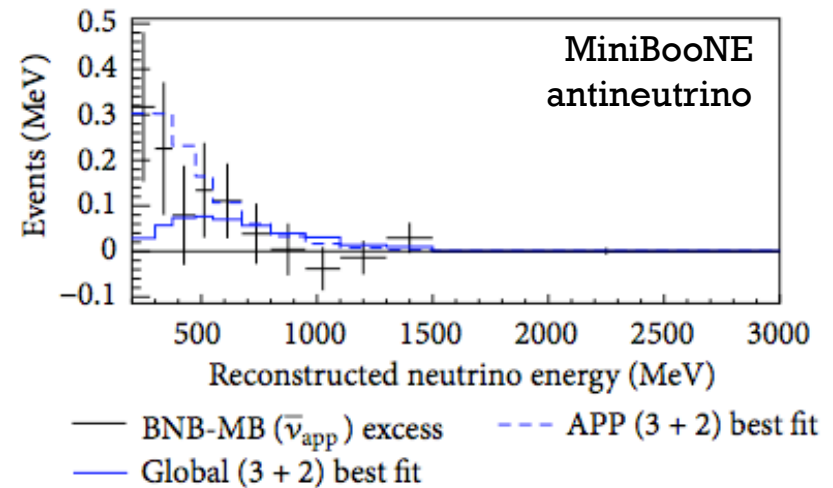
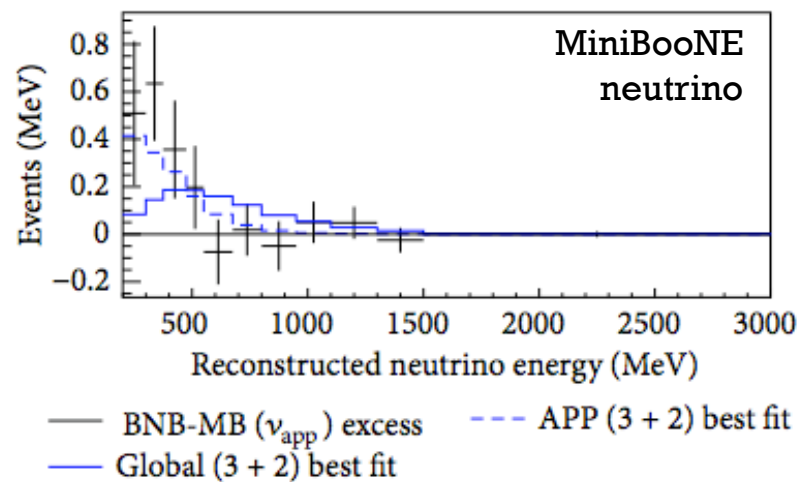
PG  $\chi^2$  (dof)  
63.8 (52)

**PG**  
**13%**

# Extended models: (1) CP violation

[Conrad, Ignarra, GK, Shaevitz, Spitz,  
arXiv:1207.4765, accepted by Advances in HEP]

(3+2) global best fit



**(3+2) with CP violation cannot explain  
MiniBooNE low E excess, unless  
we throw out disappearance  
constraints!**

# More sterile neutrinos?

## (3+3): Incompatibilities

	$\chi^2_{min}$ (dof)	$\chi^2_{null}$ (dof)	$P_{best}$	$P_{null}$	$\chi^2_{PG}$ (dof)	PG (%)
<b>3+3</b>						
All	218.2 (228)	286.5 (240)	67%	2.1%	68.9 (85)	90%
App	70.8 (81)	147.3 (90)	78%	0.013%	17.6 (45)	100%
Dis	120.3 (141)	139.3 (150)	90%	72%	24.1 (34)	90%
$\nu$	116.7 (111)	133.4 (123)	34%	25%	39.5 (46)	74%
$\bar{\nu}$	90.6 (105)	153 (117)	84%	1.4%	18.5 (27)	89%
App vs. Dis	-	-	-	-	28.3 (6)	0.0081%
$\nu$ vs. $\bar{\nu}$	-	-	-	-	110.9 (12)	53%

Conrad et al, hep-ph/1207.4765

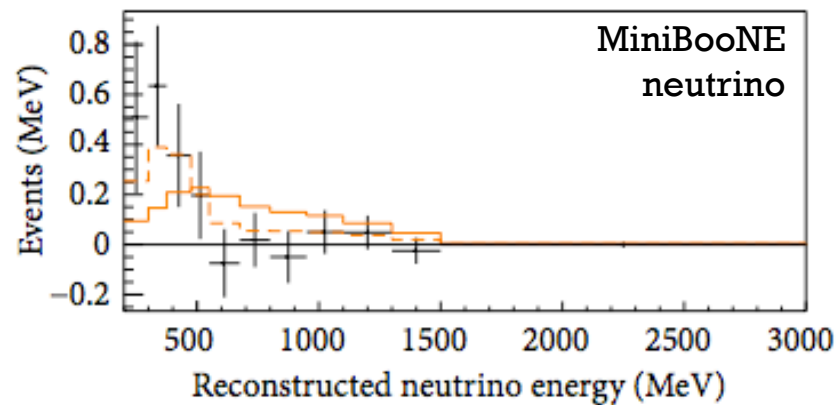
Appearance and disappearance data sets  
are incompatible under a (3+3) scenario.

PG(app,dis) with MiniBooNE removed  
from fits: 3.5%

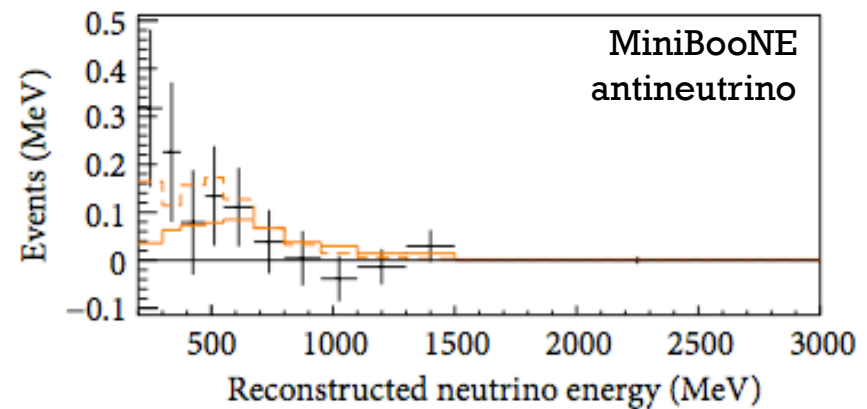
# More sterile neutrinos? (3+3): Incompatibilities

[Conrad, Ignarra, GK, Shaevitz, Spitz,  
arXiv:1207.4765, accepted by Advances in HEP]

## (3+3) global best fit



— BNB-MB ( $\nu_{\text{app}}$ ) excess    - - - APP (3 + 2) best fit  
— Global (3 + 3) best fit



— BNB-MB ( $\bar{\nu}_{\text{app}}$ ) excess    - - - APP (3 + 2) best fit  
— Global (3 + 3) best fit

MiniBooNE low energy excess is hard to  
reconcile within the global picture!

## Theoretical developments attempting to address inconsistencies:

- Fact #1:  $\nu$  vs  $\bar{\nu}$  differences

Extended sterile neutrino models with CP violation?

*Does not explain  
MiniBooNE low E excess*

- Fact #2: appearance vs disappearance differences  
“Non-standard” oscillations?



# Extended models:

## (2) Non-standard matter-like effects?

Consider a (3+1) model where:

$\nu_s$  experience matter-like potential:  $V_s = +A_s$

$\bar{\nu}_s$  experience matter-like potential:  $V_s = -A_s$

Effective matter potential in neutrino flavor space:

$$V = \begin{pmatrix} V_{CC} + V_{NC} & 0 & 0 & 0 \\ 0 & V_{NC} & 0 & 0 \\ 0 & 0 & V_{NC} & 0 \\ 0 & 0 & 0 & V_s \end{pmatrix} \simeq \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & V_s \end{pmatrix}$$

$V_s$ -dominant

Effective hamiltonian in matter:

$$H_m = \frac{1}{2E} U \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & m_4^2 \end{pmatrix} U^\dagger + V$$

$m_4$ -dominant

# Extended models:

## (2) Non-standard matter-like effects?

Consider a (3+1) model where:

$\nu_s$  experience matter-like potential:  $V_s = +A_s$

$\bar{\nu}_s$  experience matter-like potential:  $V_s = -A_s$

Gives effective mixing parameters in matter:

(as functions of  $\Delta m^2$ ,  $|U_{e4}|$ ,  $|U_{\mu4}|$ ,  $V_s$  and  $E$ )

General oscillation probability:

$$P(\nu_\mu \rightarrow \nu_e) = 4|U_{e4}^M|^2|U_{\mu4}^M|^2 \sin^2(1.27\Delta m_M^2 L/E)$$

$$\sin^2 2\theta_M = 4|U_{e4}^M|^2|U_{\mu4}^M|^2$$

$$\Delta m_M^2 = \Delta m^2 + 2EV_s$$

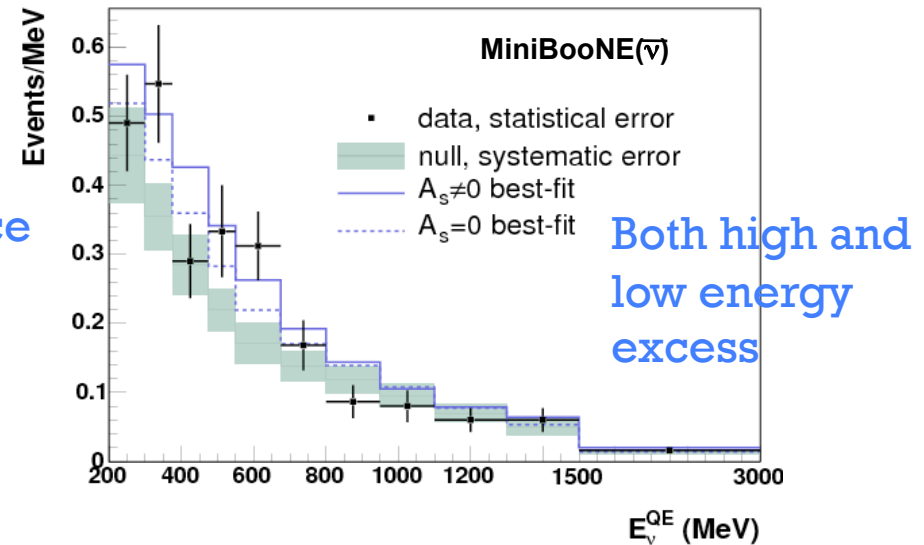
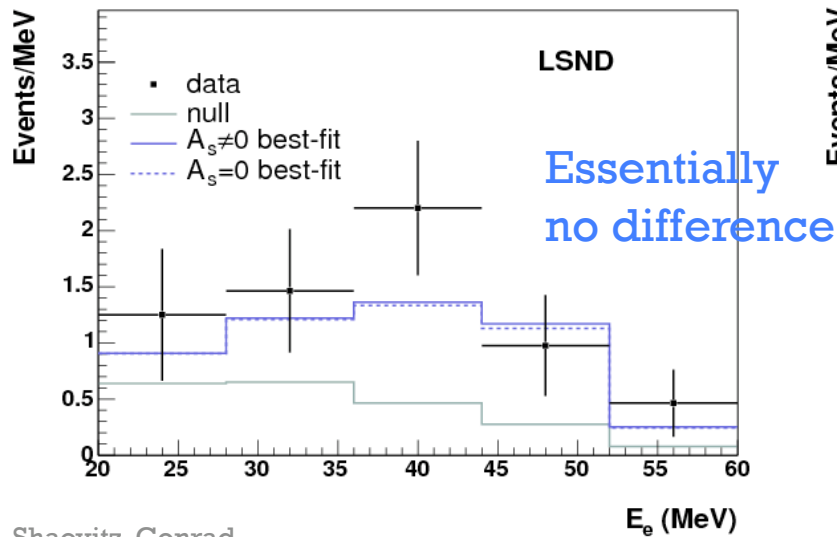
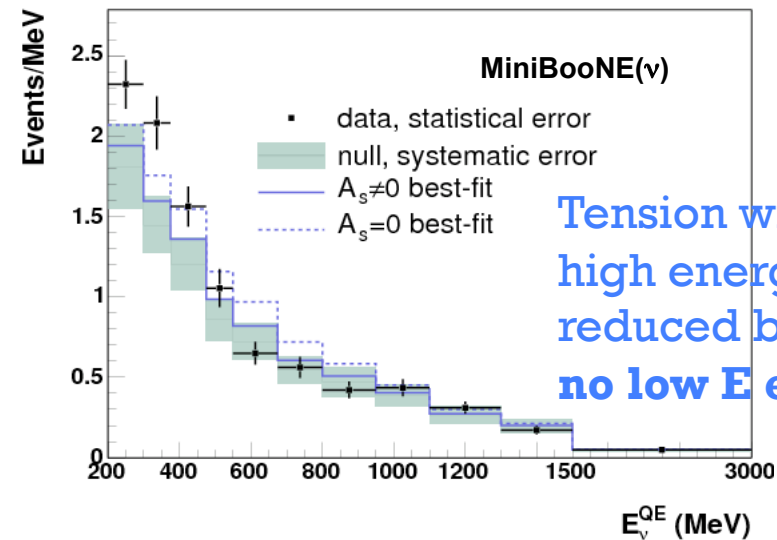
$$\sin^2 2\theta_M = \frac{16(\Delta m^2)^4|U_{e4}|^2|U_{\mu4}|^2|U_{s4}|^4}{((\Delta m^2 - 2EV_s)^2 + 4(2EV_s\Delta m^2|U_{s4}|^2))(2EV_s - \Delta m^2(1 - 2|U_{s4}|^2) + \sqrt{(\Delta m^2 - 2EV_s)^2 + 4(2EV_s\Delta m^2|U_{s4}|^2)})^2}$$

Both E- and  $\bar{\nu}/\nu$ -dependent!

# Extended models:

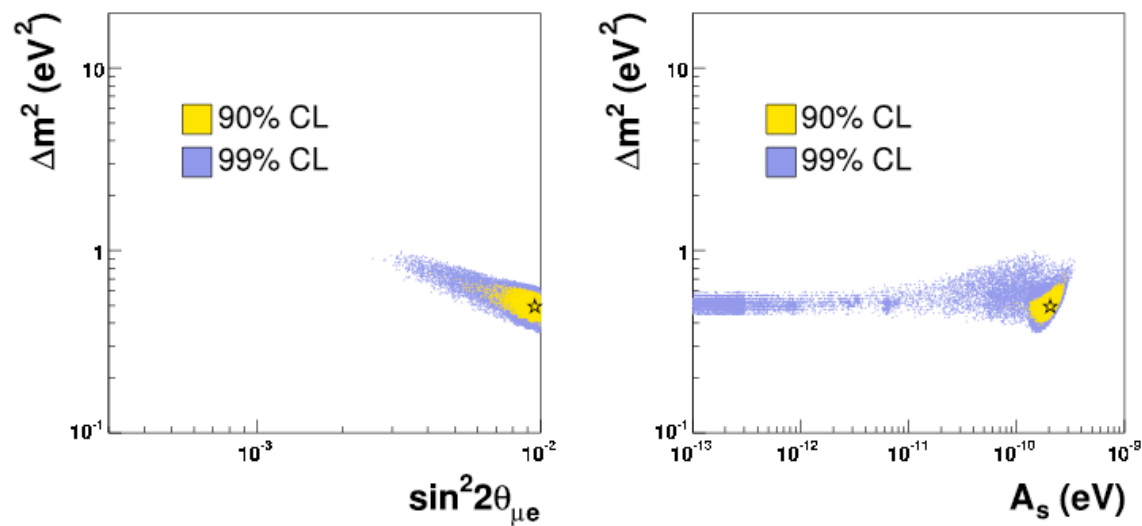
## (2) Non-standard matter-like effects?

Compatibility increases  
from 2.3% ( $A_s=0$ )  
to 17.4%, but...



# Extended models:

## (2) Non-standard matter-like effects?



Fit prefers a large  $A_s \sim 2.0 \times 10^{-10} \text{ eV}$

Best-fit vacuum oscillation parameters:

$$\Delta m^2 = 0.47 \text{ eV}^2, \quad \sin^2 2\theta = 0.01$$

( Note: for standard matter effects,  $A_e = \sqrt{2}G_F n_e \sim 10^{-13} \text{ eV}$  )

## Theoretical developments attempting to address inconsistencies:

- Fact #1:  $\nu$  vs  $\bar{\nu}$  differences

Extended sterile neutrino models with CP violation?

*Does not explain  
MiniBooNE low E excess*

- Fact #2: appearance vs disappearance differences  
“Non-standard” oscillations?

*MiniBooNE low E excess??  
difficult to interpret...*

### Other theoretical interpretations:

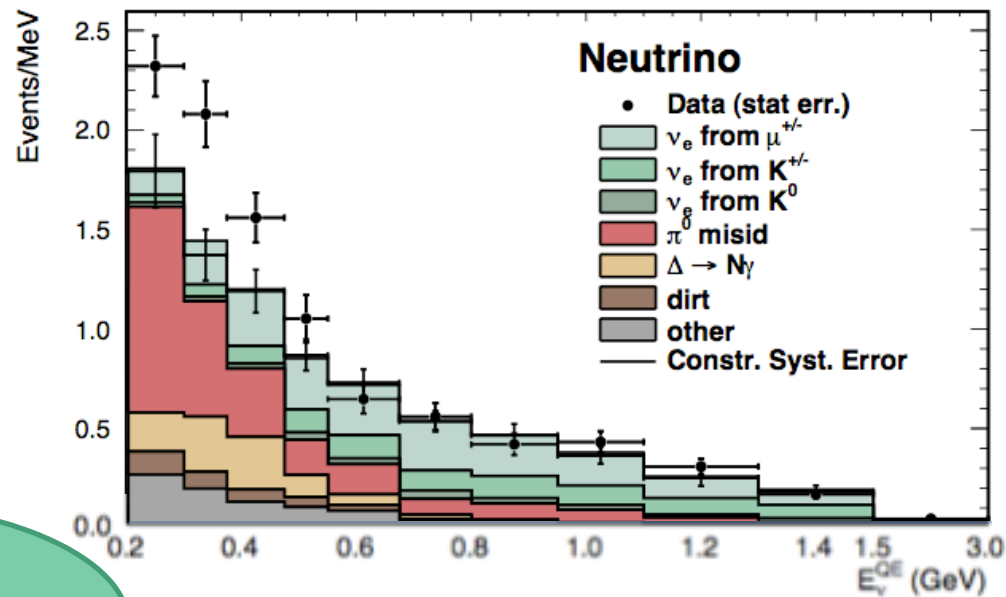
- CPT violation
- Heavy (sterile) neutrino decay
- Extra dimensions
- New interactions
- Altered neutrino dispersion relations



None of these  
provide an  
“elegant”  
solution...

# Puzzle piece #2: MiniBooNE

Low E excess: Are we missing something?



Unaccounted  
 $\nu_e/\nu_\mu$   
disappearance?

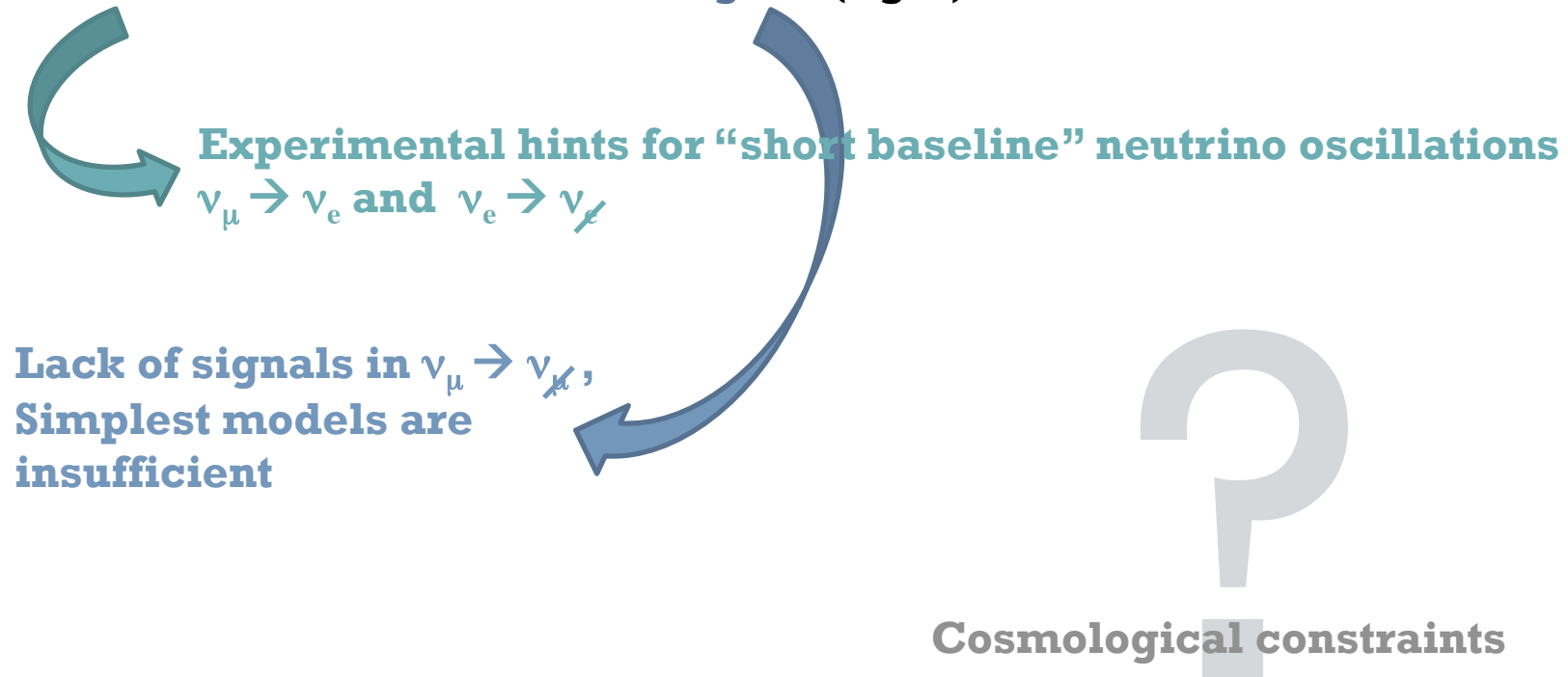
Energy  
reconstruction?  
Cross-section/  
nuclear effects?

Electron-like  
misestimated or  
new background?

Single-photon  
mis-estimated or  
new background?

# Outline

## 1. Evidence for and shortcomings of (light) sterile neutrino oscillations



## 2. Future phenomenological tests of sterile neutrino models

# Limits from cosmology

Neutrino energy density in radiation dominated era

$$\rho_\nu = N_{eff} \frac{7\pi^2}{120} T_\nu^4$$

from CMB

Affects expansion rate at that time:  $H^2(t) \simeq \frac{8\pi G}{3}(\rho_\gamma + \rho_\nu)$

Primordial element abundance:

Electron neutrinos  $\nu_e + n \leftrightarrow p + e^-$   
 determine p/n ratio  $\bar{\nu}_e + p \leftrightarrow n + e^+$

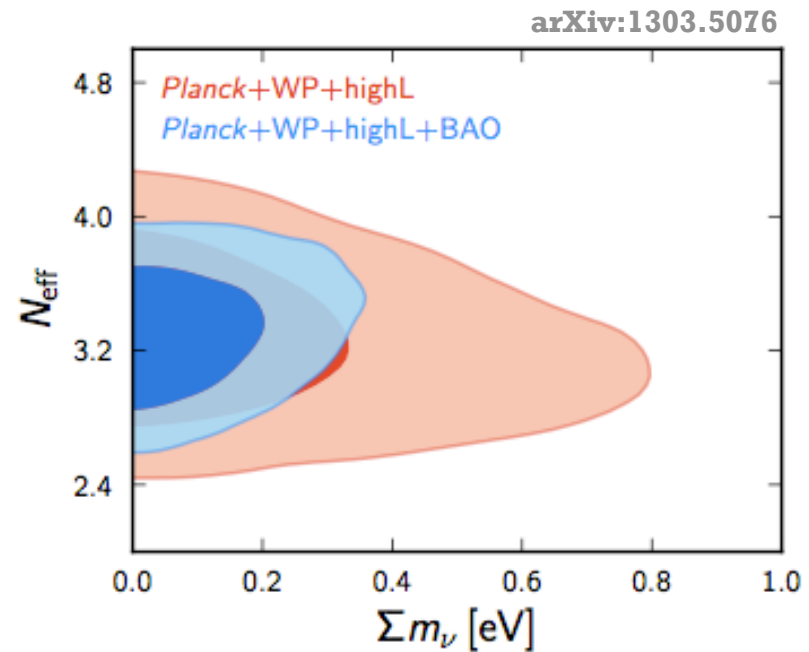
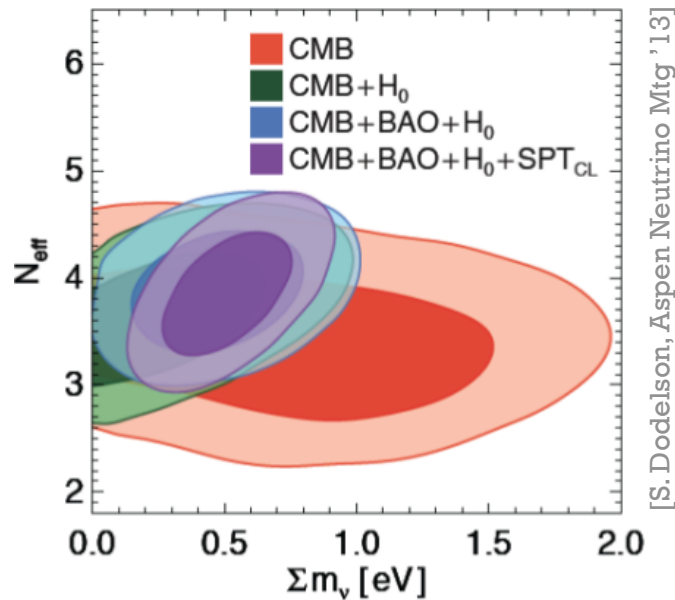
All neutrinos influence expansion rate and can alter light element abundance (mostly  $^4\text{He}$ )

CMB anisotropies and Large Scale Structure:

Insensitive to flavor content; sensitive to neutrino stress energy tensor  
 $\rightarrow N_{eff}$  and  $m_i$



# Limits from cosmology



- (1)  $N_{\text{eff}}$  somewhat compatible with additional degrees of freedom.
  - (2) Limits on  $m_s$  assuming sterile neutrinos are fully thermalized are incompatible with global fits ( $m_s > 1\text{-}2$  eV strongly disfavored).
- Limits can be evaded with further modifications to the  $\Lambda$ CDM model.*

## Currently a puzzle in neutrino physics!

50



# STERILE NEUTRINOS AT THE CROSSROADS

A Workshop  
presented by  
**The Center  
for Neutrino  
Physics**  
at Virginia Tech

September 26-28, 2011

The Inn at Virginia Tech and  
Skelton Conference Center  
Blacksburg, Virginia

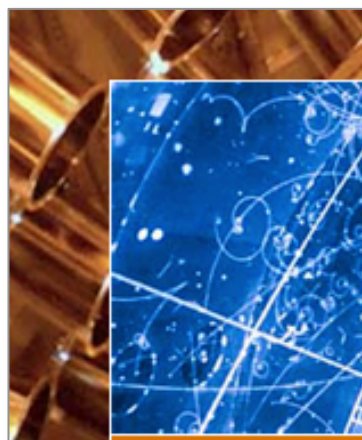
This workshop will bring  
together experts in the various  
sub-disciplines, such as  
nuclear theory (reactor fluxes,  
nucleosynthesis) and  
experiment (reactor  
experiments, flux  
measurements,  
LSND/Karmen, MiniBooNE),  
cosmology, neutrino



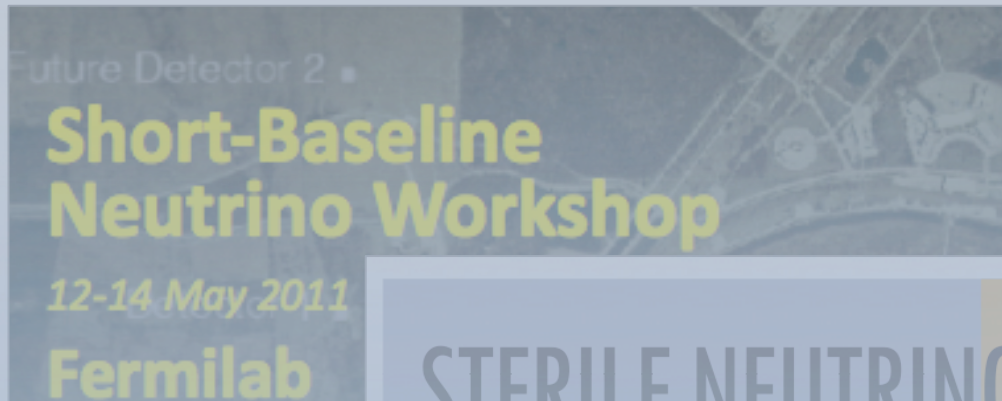
"The Crossroads" by Brent Cotton - www.cottonfinearts.com

### Light Sterile Neutrinos: A White Paper

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X. J. Ding,<sup>16</sup> Z. Djuricic,<sup>30</sup> A. Donini,<sup>31,3</sup> D. Duchesneau,<sup>32</sup> H. Ejiri,<sup>33</sup> S. R. Elliott,<sup>34</sup>  
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P. Ghoshal,<sup>41</sup> D. Gibin,<sup>44</sup> C. Giunti,<sup>45</sup> S. N. Gninenko,<sup>43</sup>  
I. Gubunov,<sup>43</sup> R. Guenette,<sup>18</sup> A. Guglielmi,<sup>44</sup> F. Halzen,<sup>46,8</sup>  
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J. J. Kopp,<sup>5</sup> V. N. Kormoukhov,<sup>55</sup> A. Kusenko,<sup>56,57</sup> P. Kyberd,<sup>58</sup>  
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J. Mariani,<sup>53,16</sup> V. A. Matveev,<sup>43,69</sup> N. E. Mavromatos,<sup>70,39</sup>  
J. Mena,<sup>3</sup> G. Mention,<sup>22</sup> A. Merle,<sup>73</sup> E. Meroni,<sup>17</sup> M. Mezzetto,<sup>44</sup>  
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P. Mumm,<sup>77</sup> V. Muratova,<sup>27</sup> A. E. Nelson,<sup>78</sup> J. S. Nico,<sup>77</sup>  
S. Mirnov,<sup>69</sup> M. Obolensky,<sup>40</sup> S. Pakvasa,<sup>80</sup> O. Palamara,<sup>18,52</sup>  
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M. Popovic,<sup>5</sup> J. Pradler,<sup>84</sup> G. Ranucci,<sup>17</sup> H. Ray,<sup>85</sup>  
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P. R. Sala,<sup>17</sup> K. Scholberg,<sup>88</sup> T. Schwetz,<sup>62</sup> M. H. Shaevitz,<sup>53</sup>  
S. Simone,<sup>91</sup> M. Skorokhvatov,<sup>92</sup> M. Sorel,<sup>3</sup> A. Sousa,<sup>93</sup>  
J. Stancu,<sup>44</sup> I. Stancu,<sup>28</sup> A. Suzuki,<sup>95</sup> T. Takeuchi,<sup>16</sup> I. Tamborra,<sup>96</sup>  
J. J. T. A. Tonazzo,<sup>40</sup> C. D. Tunnell,<sup>100</sup> R. G. Van de Water,<sup>34</sup>  
J. Vignoli,<sup>52</sup> M. Vivier,<sup>22</sup> R. B. Vogelaar,<sup>16</sup> M. O. Wascko,<sup>63</sup>  
J. Y. Y. Wong,<sup>25</sup> T. T. Yanagida,<sup>27</sup> O. Yasuda,<sup>103</sup>  
W. Yokley,<sup>16</sup> G. P. Zeller,<sup>5</sup> L. Zhan,<sup>61</sup> and H. Zhang<sup>62</sup>



THE 4<sup>TH</sup> NEUTRINO



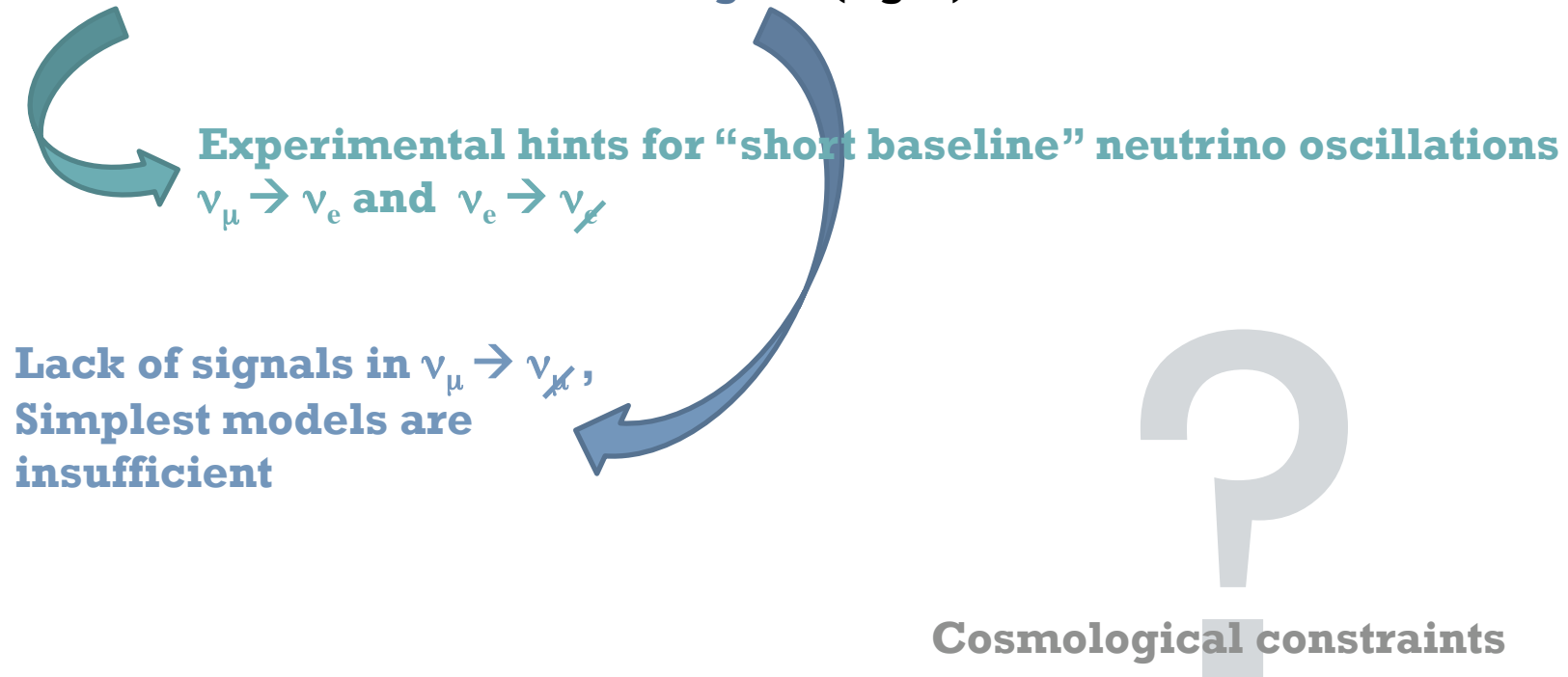
What do we need to address the question of sterile neutrinos?

- (a) New physics models
- (b) Better statistical treatment of global fits
- (c) New, definitive experimental tests
- (d) All of the above



# Outline

## 1. Evidence for and shortcomings of (light) sterile neutrino oscillations



## 2. Future phenomenological tests of sterile neutrino models



# Accelerator-based experiments:

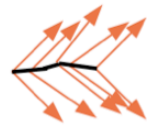
- MINOS+ (funded)
- MiniBooNE+ (proposal)
- MicroBooNE (funded)
- LAr1 (proposal in preparation)
- NESSiE (proposed)
- $\nu$ STORM (LOI)

$\nu_\mu$  or  $\nu_e$  beams, can search for  $\nu_\mu$  or  $\nu_e$  disappearance  
and/or  $\nu_\mu \rightarrow \nu_e$ ,  $\nu_e \rightarrow \nu_\mu$  appearance

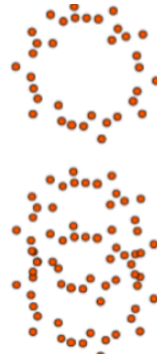
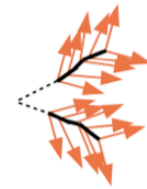
- Primary physics goal:  
Investigate the nature of  
the **MiniBooNE low  
energy excess**
- Is the excess due to **e** or  **$\gamma$** ?

**Single e** and **single  $\gamma$**   
are indistinguishable in  
a cherenkov detector...

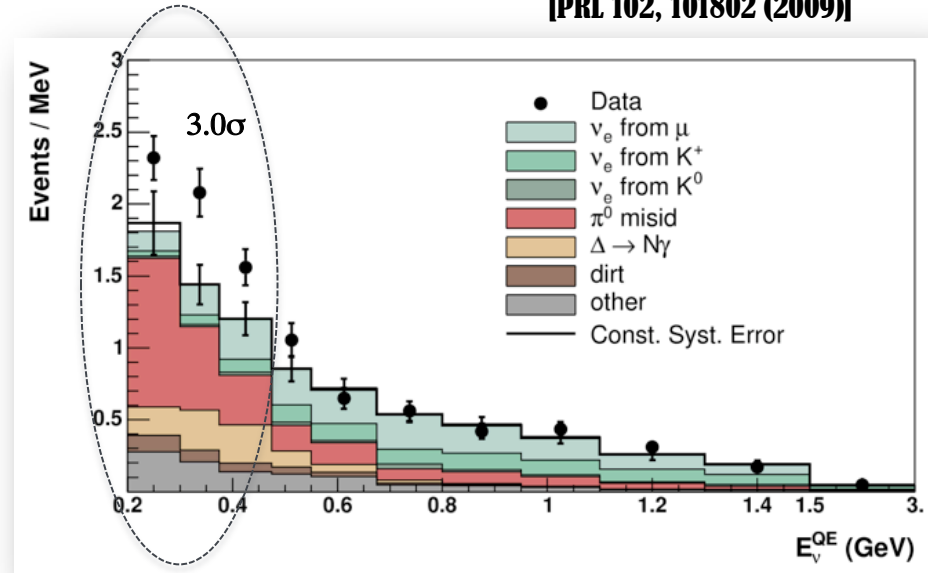
electron:  
short track,  
multiple scattering,  
bremsstrahlung



photon(s):  
photoconversion  
→ electron-like track(s)

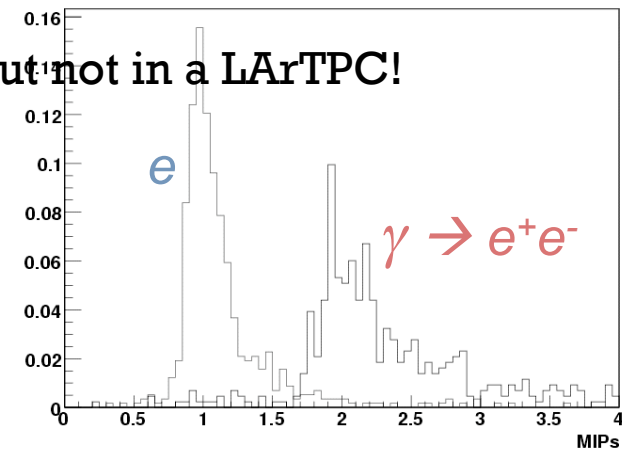


**MiniBooNE unexplained “low energy excess”  
[PRL 102, 101802 (2009)]**



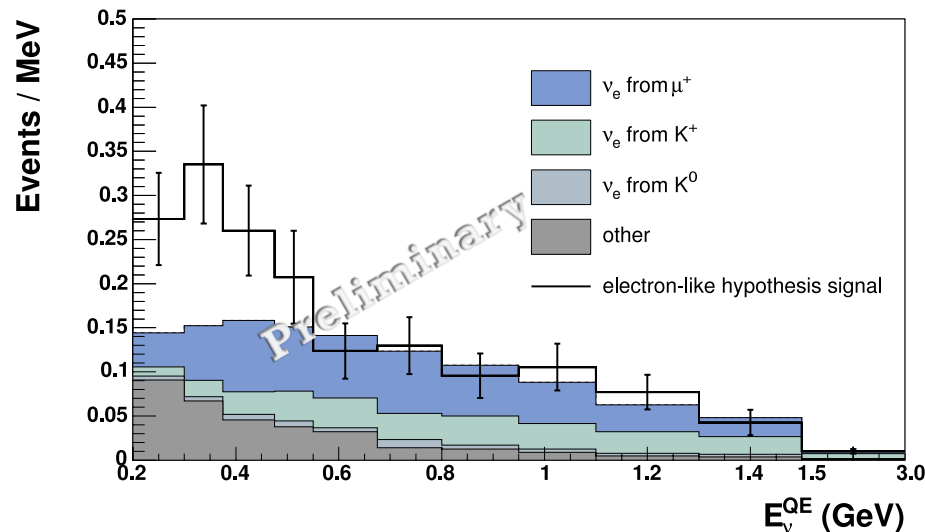
**Energy loss in first 24mm of track:  
250 MeV electron vs. 250 MeV photon**

...but not in a LArTPC!



## “Low E excess”:

What MicroBooNE expects to see if excess is due to **single e**

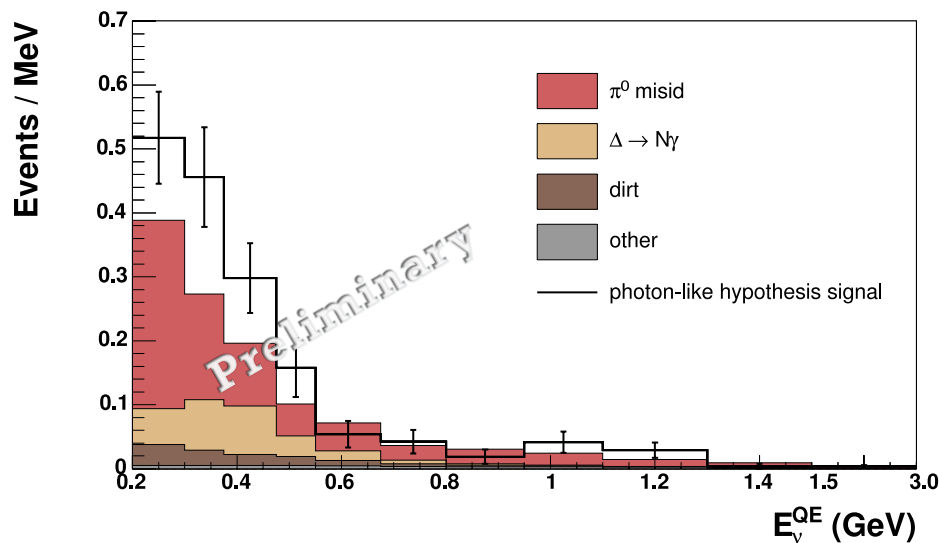


Possible explanation:  
 $\nu_\mu \rightarrow \nu_e$  nonstandard  
oscillations  
(sterile neutrinos, extra  
dimensions, NSI,...)

About **37 excess events** above a background of 45 events  
→  **$5.7\sigma$  statistical significance**

## “Low E excess”:

What MicroBooNE expects to see if excess is due to **single  $\gamma$**



Possible explanation:  
background  $\gamma$  or  $\pi^0$  or  
“new” single photon  
production

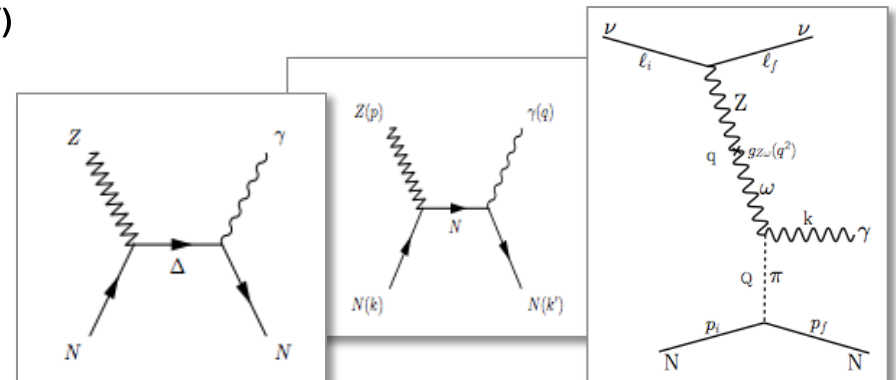
e.g.

R. Hill arXiv: 0905.0291

Jenkins et al arXiv:0906.0984

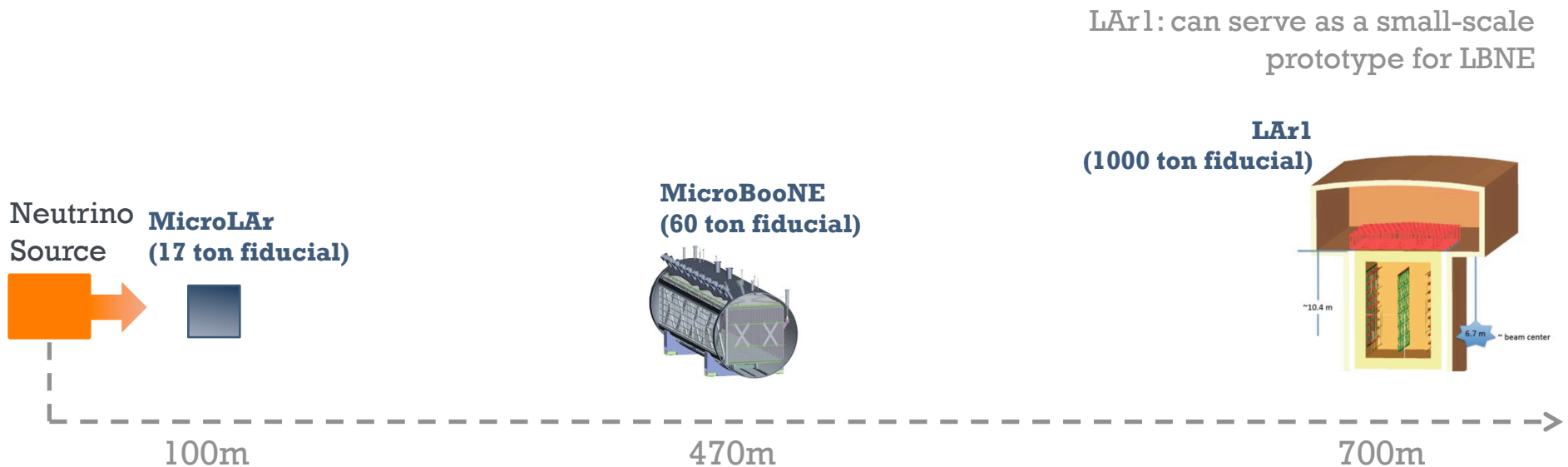
Serot et al arXiv: 1011.5913

About **37 excess events** above a  
background of 79 events  
 $\rightarrow$   **$4.1\sigma$  statistical significance**

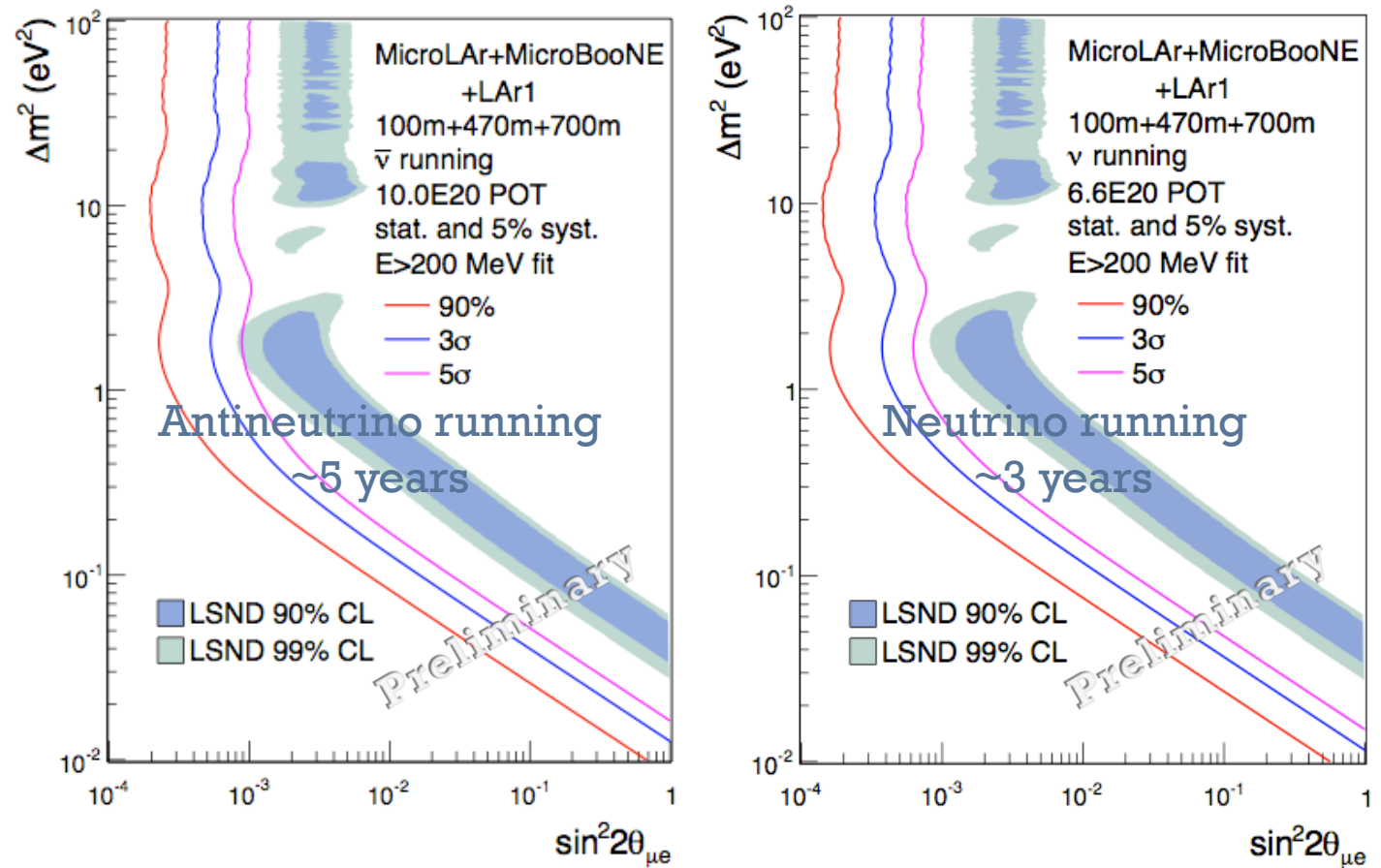




- A second and third LArTPC placed in the Booster Neutrino Beam at Fermilab, in line with MicroBooNE
- Near/far comparison for short-baseline oscillation search
- **Definitive test of MiniBooNE/LSND anomalies**



- **Physics reach:** Definitive ( $5\sigma$ ) test of LSND and MiniBooNE in both neutrino and antineutrino modes

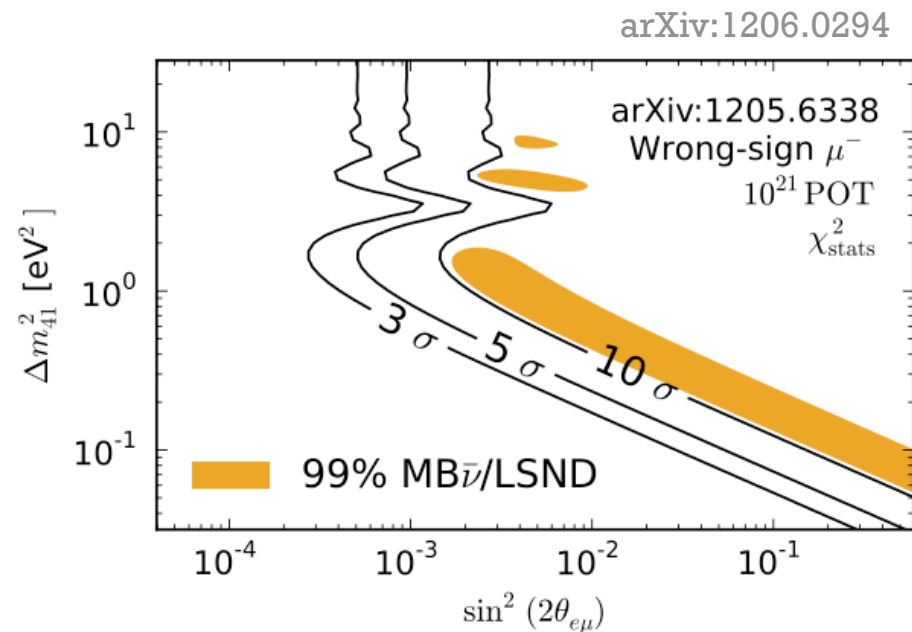
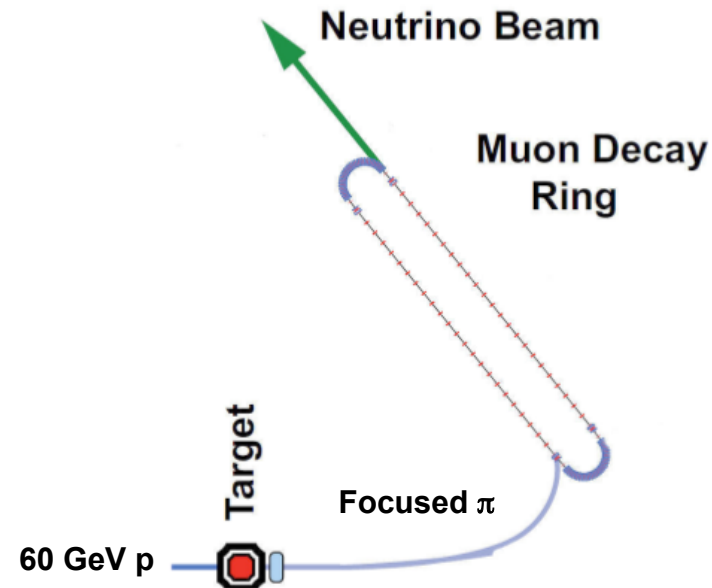


- Also  $(\bar{\nu}_e)$  and  $(\bar{\nu}_\mu)$  disappearance

# NuSTORM

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- Neutrinos from STORed Muons
- $\nu_e$  flux from  $\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e$
- $\nu_e \rightarrow \nu_\mu$  appearance
- 3.8 GeV/c muons and 1.3kton sign-selecting (MINOS-style) detector at 2km →  
10 sigma sensitivity to MiniBooNE/LSND !
- Also,  $\nu_e$  disappearance



# Decay-At-Rest experiments:

- OscSNS
- Super-K
- K-DAR

$\nu_\mu$  and  $\nu_e$  isotropic fluxes,  
can search for  $\nu_\mu \rightarrow \nu_e$  appearance,  
and  $\nu_e$  disappearance,  $\nu_\mu$  disappearance

## Reactor-based experiments:

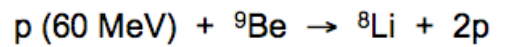
- SCRAAM
- Nucifer
- Stereo

## Radioactive source experiments:

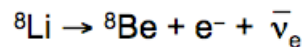
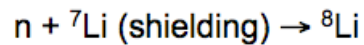
- Borexino, Ce-LAND, Daya Bay
- Borexino, SNO+Cr
- RICOCHET
- IsoDAR

Lower E  $\nu_e$  isotropic flux, can search for  $\nu_e$  disappearance

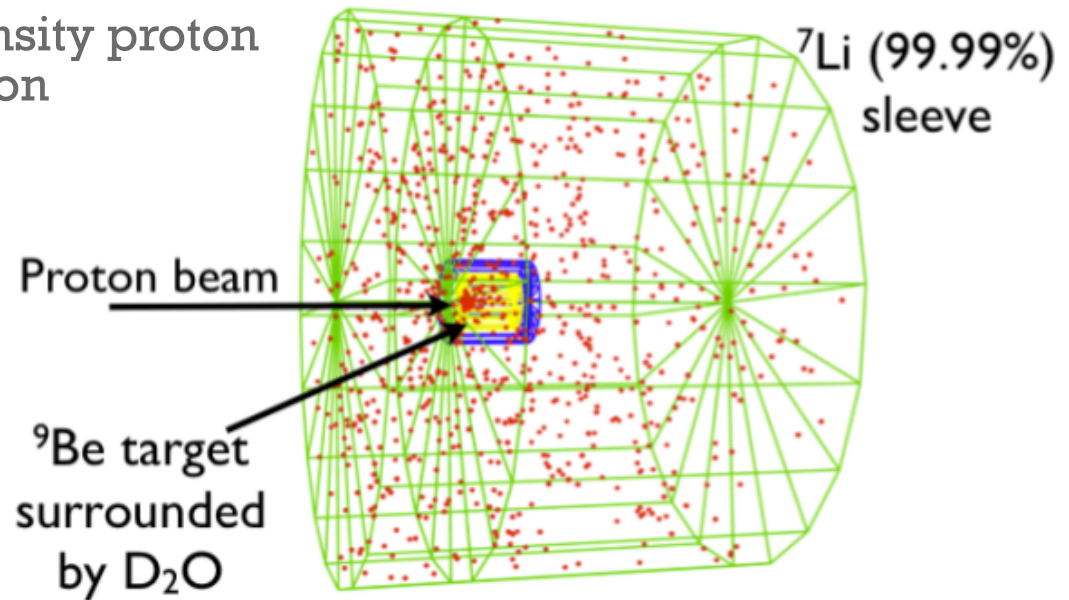
- **New idea:** High intensity nuebar source from  $^8\text{Li}$   $\beta$ -decay and liquid scintillator/water detector (e.g. Kamland)
- $^8\text{Li}$  produced by high-intensity proton beam from 60MeV cyclotron



- plus many neutrons since low binding energy

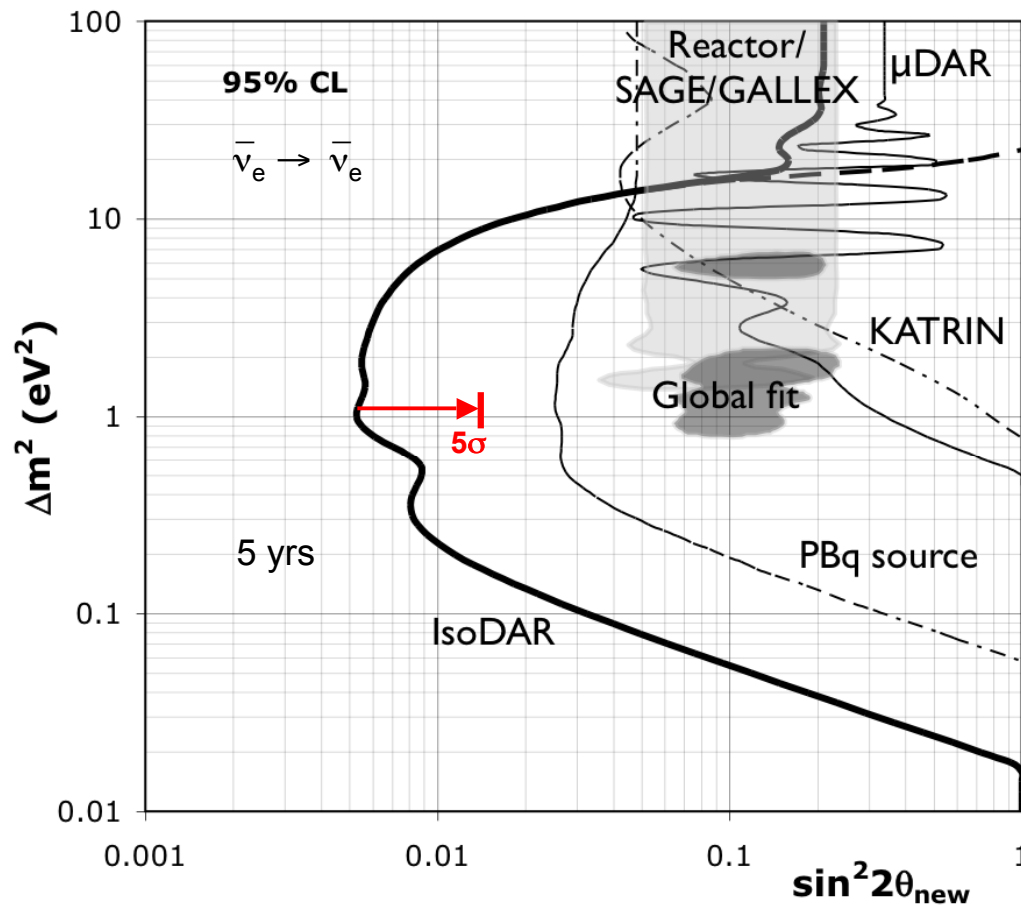


- Mean  $\bar{\nu}_e$  energy = 6.5 MeV
- $2.6 \times 10^{22} \bar{\nu}_e / \text{yr}$

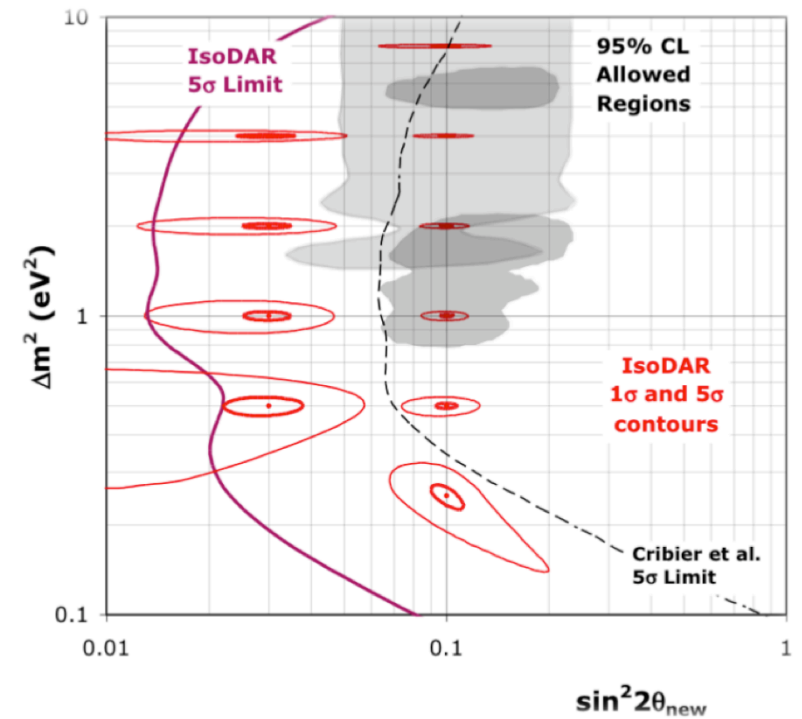


- Nuebar disappearance and oscillatory behavior vs L/E
- **Definitive test of reactor anomaly**

IsoDAR  $\bar{\nu}_e$  disappearance oscillation sensitivity (3+1):

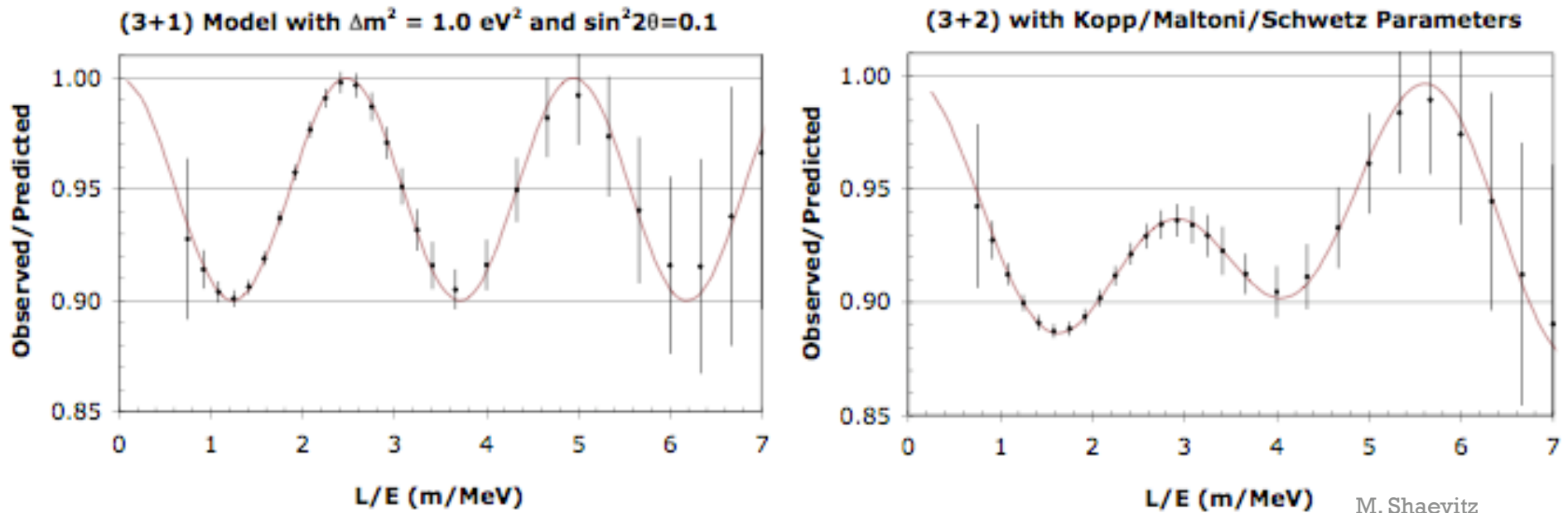


M. Shaevitz



5σ (discovery) sensitivity to parameters  
 allowed by short-baseline reactor measurements!

Observed/Predicted event ratio vs L/E including energy and position smearing



M. Shaevitz

IsoDAR's high statistics and good L/E resolution:  
potential for distinguishing between  
simple (left) and more complicated (right) sterile neutrino oscillation models.



# End remarks

Theoretical motivation for light ( $\sim 1$  eV) sterile neutrinos is perhaps not so strong, though sterile neutrinos with sizable mixing emerge in several models of neutrino mass (heavy sterile neutrinos...).

Their discovery would point towards new physics.

“...their role is relevant enough to justify an open mind attitude and a close look for any, yet tiny, evidence for new effects beyond the *too much* successful Standard Model.”

[Theorist Anonymous]

Experimental hints may be right in front of us, albeit not completely understood. Need new, definitive experiments. Model-independent searches should be given highest priority.

Thank you!